"In the name of God, the merciful, the compassionate"

# Modelling tidal processes in the Persian Gulf - With a view on Renewable Energy -

Dissertation with the aim of achieving a doctoral degree at

The Faculty of Mathematics, Informatics and Natural Sciences Institute of Oceanography University of Hamburg

> Submitted by Hossein Mashayekh Poul 2016 in Hamburg

Day of oral defense: 27.05.2016

The following evaluators recommend the admission of the dissertation:

Prof. Dr. Jan Backhaus

PD. Dr. Thomas Pohlmann

"And it is He who has released [simultaneously] the two seas, one fresh and sweet and one salty and bitter, and He placed between them a barrier and prohibiting partition."

Allah, years: 609-632, Al-Forghan 53, Quran

## Abstract

The main semidiurnal (M2 and S2) and diurnal (K1 and O1) tidal constituents were simulated in the Persian Gulf (denoted PG). The topography of the PG was discretized on a spherical grid with a resolution of 30 seconds in both latitude and longitude. It included coastal areas prone to flooding. The model permitted flooding of drying banks up to 5 meters above mean sea level. At the open boundary, it was forced by 13 harmonic constituents extracted from a global tidal model. The Model results agreed well with tide gauge observations. Co-tidal charts and flow extremes were presented for each tidal constituent. The co-tidal charts showed two amphidromic points for semidiurnal and one for diurnal tidal constituents. Maximum tidal amplitudes were obtained in the north-western part of the PG, where coastal flooding prevails in wide areas. Strong tidal currents occurred in the PG but their locations are driven by different, dominant tidal constituents. Maximum velocities were found in shallow regions. Particularly high amplitudes of elevations and high velocities of currents were found in the canal between Qeshm Island and the mainland. Tidal rectification around Qeshm Island influenced hydrodynamics across the PG, as far as the coast of Saudi Arabia and the northern part of the PG. The results provided a good estimate of the annual kinetic energy output for the PG on the Iranian side, for the entrance of Musa estuary and Qeshm canal.

Geological studies in the PG have revealed the existence of sub-seabed salt-domes. Suitable, high-pass filtering of the PG seabed topography revealed the signature of these domes on the seabed, i.e. numerous hills and valleys with amplitudes of several tens of meters and radii from a few up to tens of kilometers. It was suspected that the 'shark skin' of the PG seabed may affect the tidal residual flow. The interaction of tidal dynamics and these obstacles was investigated in a non-linear hydrodynamic numerical tidal model of the PG. First, the model was used to characterize flow patterns of residual currents generated by a tidal wave passing over symmetric, elongated and tilted obstacles. Thereafter, it was applied to the entire PG. The model was forced at its open boundary by the four dominant tidal constituents residing in the PG. Each tidal constituent was separately simulated. Tidal residual currents in the PG, as depicted by Lagrangian trajectories, revealed a stationary, eddy-rich flow. Each eddy can be matched with a topographic obstacle. This confirmed that the tidal residual flow field is strongly influenced by the nonlinear interaction of the tidal wave with the bottom relief which, in turn, is deformed by salt-domes beneath the seabed. Different areas of maximum residual current velocities were identified for each type of tidal constituent. Two main cyclonic gyres and several adjacent gyres rotating in opposite directions and a strong coastal current in the northern PG were identified.

The non-linear hydrodynamic numerical tidal model was applied to investigate the tidal resonance in the PG. The model was used to characterize the amplified response of the basin to different forcing periods. It was forced by waves with the same amplitude but different periods ranging from 3.5 to 35.5 h with increments of 0.5 hours at its open boundary to the Oman Sea. Each wave was simulated separately. The results revealed that, in three areas, tidal elevations were significantly larger than the forcing amplitude, indicating resonance. These areas were the northern PG (maximum Amplification Factor (AF) = 1.61), the Strait of Hormuz (maximum AF = 3.00), and the southern PG (maximum AF = 1.33). The amplification factor (AF) is the ratio of local amplitudes vs. forcing amplitude. Diurnal tides were resonant in both the northern and southern PG. Semidiurnal constituents were amplified in the northern Gulf as well as in the Strait of Hormuz. A simulated sea level rise due to climate change of 1 meter increased the AF off the Arabian coast for semidiurnal tides from 0.72 to 1.21. In the Qeshm Canal in the Strait of Hormuz, AF increased from 1.36 to 1.57 for semidiurnal and from 0.73 to 1.1 for diurnal tides. The results provide a good estimate of the annual potential energy output for the PG on the Iranian side, for the Musa estuary and Qeshm canal.

The tidal barotropic residual circulation in the Musa estuary was described by applying a non-linear, 3-d hydrodynamic numerical model. The main point was to consider the effect of evaporation on density-driven circulation and interactions with tidal currents. The Musa estuary is located in the north-west of the PG. The climate in this region is arid, resulting in an excess of evaporation over precipitation. There is no river runoff in this estuary. The results suggested that the structure of the residual circulation and stratification depended on

the evaporation rate and, of course, the difference in tidal amplitude, i.e. neap and spring tide. As a result of evaporation, the residual circulation was vertically stratified, with a dense, saline, near-bottom flow toward the PG and relatively fresh inflow at the surface. But, in scenarios using tides, residual circulation occurred in the opposite direction. The results revealed a high salinity outflow and a lower salinity inflow but a stable salinity across the whole region. There was a horizontal gradient in tidally-averaged salinity with the salinity increasing towards the head of the Musa estuary, which is a salt producing, coastal system.

# Table of Contents

Model	ling tidal processes in the Persian Gulf	. 1
Abstra	ct	. 3
Table of	of Contents	. 6
Motiva	tion, Objectives, and General Approach	. 8
Chapte	r 1	.9
1.1	General Introduction	.9
1.1.1	Topography, Morphology and Bathymetry of the PG	.9
1.1.2	Meteorology	11
1.1.3	Tides	12
1.1.4	General circulation	13
1.2	Model Description	14
1.2.1	VOM and HAMSOM	15
1.2.2	VOM-SW2D and 3D	17
Chapte	er 2	18
2 T	he PG Tide Model	18
2.1	Setup and Forcing Data	18
2.2	Model Evaluation	20
2.3	Tide in the PG	24
2.4	Kinetic energy	32
2.5	Effect of Qeshm Canal	33
Chapte	r 3	35
3 TI	he PG Tidal Residual Currents	35
3.1	Topography and circulation in the PG	35
3.2	Residual flow	37
3.3	Model Description and Methods	37
3.4	Results	39
3.4.1	Residual current in an experimental domain	39
3.4.2	Residual current in the PG	42
Chapte	er 4	50
4 Ti	idal Resonance in the PG	50
4.1	The PG	50
4.2	Tidal Resonance	52
4.3	Model Description	53
4.4	Tidal resonance in the PG	53
4.5	Potential energy	60
Chapte	r 5	62

5 High evaporation and inverse estuary of the PG	62				
5.1 Musa estuary					
5.2 Model Description and Methods	63				
5.3 Results	67				
5.3.1 Experimental domain	67				
5.3.2 Musa estuary	70				
Chapter 6					
6 Summary and Conclusions	78				
Acknowledgement	81				
Declaration	82				
Bibliography	83				
Appendix	90				
1 Theoretical Aspects of 2D primitive equation models	90				
1.1 Influence of the Spatial Discretization on Wave Propagation	90				
1.2 Spatial Discretisation for the 'Primitive' Equations	91				
1.3 Numerical Wave Dispersion in Arakawa C-Grid	92				
1.4 Dispersion Relations of Arakawa C-Grids	92				
2 Rotational Primitive Equation Models; explicit, implicit	93				
2.1 Explicit Scheme for the Storm Surge Model in the Arakawa C-grid	94				
2.2 The implicit Storm Surge Model	95				
2.3 Horizontal Momentum Diffusion					
2.4 Boundary Conditions for the Laplacian; Slip-conditions					
2.5 Coriolis Rotation; the Problem with spatial averaging in the C-grid					
2.6 The Lagrangian upstream Advection Scheme, LAS:	104				
2.7 Non-linear advective Terms in the Equations of motion	105				
2.8 Stability of the rotational nonlinear 2D C-grid model	106				
3 Implicit Channel Model with 'Movable' Boundary	106				
3.1 Flooding towards the west					
3.2 Flooding towards the east					
List of Figures					
List of Tables1					
List of publications1					

# Motivation, Objectives, and General Approach

The dynamics of tidal basins include a wide range of features with different spatial and temporal scales. Numerical simulation of the Persian Gulf (PG) and its estuaries become an interesting area of research. The simulations are performed by the development of sophisticated ocean model suitable for this region of complex circulation. Such research is important because many basic questions regarding physical processes in the PG remained unanswered; e.g. tidal resonance and tidal residual currents and effects of evaporation on the shallow tidal flat in the northern estuary of the PG, Musa estuary. Moreover, as tidal waves move an enormous volume of water twice a day, for semidiurnal constituents, they provide a great amount of renewable energy.

A numerical model is able to simulate tidal processes, with having the precise geometrical features of the flow domain. Potential errors in numerical models result from incomplete geometries, including simplification of coastal and bed irregularities as well as ignoring small islands, particularly along the coastal zone. These deficiencies are important especially in the study of residual currents. The present simulation, with the highest resolving grid used for tidal predictions in the PG compared to various studies, can describe tidal residual currents realistically and produces more accurate results for the other tidal processes by considering more geometrical complexities.

The main purpose of this study is to improve the understanding of important features of tidal dynamics and thermodynamics; with a view of tidal renewable energy. The thesis is organized as follows: Chapter 1 presents an overview of Topography, Bathymetry and Morphology, Meteorology, Tides and General circulation of the PG. Theory and Methods are also described in this chapter together with a general description of VOM. The model evaluation is described in chapter 2 and comparisons demonstrate the agreement of the model data with available measurements. Furthermore, results of the tidal simulation by VOM-SW2D is presented in this chapter from two published papers of this study, description (Mashayekh Poul et al., 2016) and energy of tide (Mashayekh Poul et al., 2014) in the PG. Analyses of the model results including Tidal Residual Current (paper in revision in JGR) are discussed in chapter 3. Tidal Resonance in the PG is explained in chapter 4 and investigation of the inverse estuary in the northern PG in chapter 5. Finally, Chapter 6 summaries the main findings and presents an outlook for future studies and developments.

## Chapter 1

#### 1.1 General Introduction

Understanding tidal dynamics is important for coastal safety, navigation, ecology and nowadays for Renewable Energy. The tide in semi-enclosed basins is the result of cooscillation with a larger sea, where basin geometry and topography play an important role. The region of interest that is analysed in this study is the PG. For a better understanding, a short description of the physical properties of the PG is given in the following sections.

#### 1.1.1 Topography, Morphology and Bathymetry of the PG

The PG, sometimes incorrectly called the Arabian Gulf, is a shallow semi-enclosed marginal sea located between Iran and the Arabian Peninsula (Figure 1). It is connected with the Indian Ocean through the Strait of Hormuz. The length of the PG is about 1000 km in Northwest to Southeast orientation; the width varies from a maximum of 338 km to a minimum of 56 km in the strait. The coastal orography bordering the PG exhibits distinct contrast: while the Iranian coast is mountainous, the Arabian coast is mostly desert except around the Strait (Yao, 2008).

The bottom topography of the PG is dominated by soft sediments at the sea floor. It is generally deeper near the Iranian coast and is deepest near the opening of the Strait of Hormuz. The average depth of the topography has reported 35-36m (Badri and Wilders, 2012; Moeini et al., 2010; Ranaee et al., 2011; Reynolds, 1993; Thoppil and Hogan, 2010a). This basin is a relatively shallow zone near the closed end, extended all the way along the southern part of the basin, roughly connected to one deeper part, with a clearly asymmetric cross-sectional depth profile of the center part. Maximum depth in the deeper part is 80 m,

except in the Straits of Hormuz where depths in excess of 100 m are found (Pous et al., 2004a; Roos and Schuttelaars, 2010).



Figure 1: Bathymetry of the PG region (numerical model domain). The present model forced at the southern open boundary.

The coastal boundary and the bottom topography of the PG are very irregular and several islands of various sizes and shapes are spread over the region (Sabbagh-Yazdi et al., 2007). From geological studies in this area it is known that in the southern basin of PG there are numerous salt domes of circular shape, while in the northern basin they mostly have an elliptical shape and are connected by elongated ridges (Edgell, 1991; Perotti et al., 2011; Sarnthein, 1972; Seni and Jackson, 1984; Thomas et al., 2015; Zaigham et al., 2013). Holocene sediments in the PG are primarily carbonates. Shallow salt domes form mounds on the seafloor, and particularly active diapirs form islands exposing salt at the surface (Kent, 1979; Purser, 1973). Under marine conditions, sand can accumulate by winnowing on bathymetric shoals. Consequently, Salt domes having sufficient surface expression are overlain by sand-rich sediments. Small reefs might also be expected on topographic highs over dome crests. Such dome crest reefs have been recognized in the PG (Purser, 1973; Seni and Jackson, 1984).

Purser 1973 subdivided bathymetric Highs in the PG which have been grouped into three classes: outer (basin center), intermediate and inner (coastal).

- 1. The central parts of the basin, where water depths generally exceed 50 m, are characterized by numerous highs with marked vertical relief. Many of them are salt diapirs and they have a structural origin. The latter is generally symmetric in outline and range from islands to submerged shoals. All have one feature in common; they are surrounded by relatively deep water.
- 2. The sloping sea floor is characterized by a great variety of marine highs and depressions. They vary in diameter from several hundred meters to more than 50 km. Many emerge as islands due to salt diapirism in the Southeastern parts of the PG. Others are low sand cays whose origins are essentially sedimentary. A limited number are emergent pre-Holocene mesas. All have one feature in common: they are surrounded by relatively shallow water varying in depth from 36m on the outer parts of the homocline to less than 9m near the coast.
- 3. Highs situated close to the mainland shoreline may considerably affect coastal sedimentation. They constitute low islands and shoals surrounded by complex patterns of reefs and sand bars. Most highs have a pre-Holocene core of "miliolite" limestone around which sediments are accreting.

#### 1.1.2 Meteorology

The PG lies in the subtropical region where most of the Earth's deserts are to be found and where the boundary of the tropical circulations and the synoptic weather systems of midlatitudes are located. The seasonal shifting of the two weather systems leads to strong seasonal variability in near-surface meteorological conditions. The surface air temperature at the northern PG, for instance, changes from 15°C in winter to 34°C in summer (Reynolds, 1993; Yao, 2008). The region is arid leading to considerable evaporation, greatly exceeding precipitation and river discharge (Al-Subhi, 2010; Pous et al., 2004b).

The most well-known, and notorious, weather phenomenon in the PG is the Shamal. This surface wind in the PG navigated by the mountains along the Iranian coast is predominantly northwesterly throughout the year, i.e. along the axis of the PG (Reynolds, 1993). The characteristics of the two seasons Shamals are markedly different (Perrone, 1979). During winter, mainly between November and February, the wind is slightly stronger than that during the summer, between June and September (Blain, 1998, n.d.). The summer Shamal is continuous. It is associated with the relative strengths of the Indian and Arabian thermal lows.

The winter Shamal has a shorter duration compares to summer Shamal. It is associated with frontal passages of the synoptic weather systems, bringing cold air over the PG from higher latitudes. It is accompanied by such adverse weather conditions as thunderstorms, turbulence, low visibilities, and high seas (Perrone, 1979; Reynolds, 1993). The cold and dry air originating from the northwest during winter leads to extreme evaporation which results in high salinity and density of the PG water (Blain, 1998, n.d.; Thoppil and Hogan, 2010a). There are two types of winter Shamal with respect to duration, those which last 24–36 h and those which last for a longer period of 3–5 days (Thoppil and Hogan, 2010a). Shamal wind generated storm surges, coupled with tidal effects can lead to significant changes in the sea level of several meters (El-Sabh and Murty, 1989).

The different diurnal heating and cooling cycles over the PG and the surrounding land induce a strong breeze along the entire coastline, especially along the Arabian coast. One effect of these winds is to drive surface pollutants to the beach much faster than they would move otherwise (Reynolds, 1993).

#### 1.1.3 Tides

Tides are an important and permanent driving force in the PG. The safe navigation of ships through shallow water ports, estuaries and harbor engineering projects requires knowledge of the time and height of the tides as well as the speed and direction of the tidal currents. Also, depending on the species and water depth in this region fish may concentrate during ebb or flood tidal currents. Finally, extracting energy from the tidal waves is important because of its significant advantage.

During the last decade, a number of models have been applied for studies of tidal dynamics in the PG (Bosch van Drakestein, 2014; Ganj, 2013; Gorji-Bandpy et al., 2013; Pous et al., 2013; Sabbagh-Yazdi et al., 2007). In general, tides in the PG are complex. The dominant tidal pattern changes from being primarily semidiurnal to diurnal (Reynolds, 1993). The leading tidal constituents in this area are M2, K1, S2, O1, N2, P1, K2, and Q1; from biggest to smallest. This order may change with the F-factor at other locations in the domain. The F-factor identifies the type of tide between diurnal, semidiurnal and mixed. It is defined as the ratio of the main diurnal over the main semidiurnal constituent's amplitudes. For the PG, it is K1+O1 for diurnal and M2+S2 for semidiurnal amplitudes (Najafi, 1997).

The PG has a natural period of 22.6 or 21.7 hours for tidal waves based on Japanese method and Chrystal method (Defant, 1961), respectively. The semidiurnal and diurnal waves generate resonant interactions in the domain. The result from these interactions is a system of

amphidromic points of Kelvin-Taylor type (Pous et al., 2013), two points for semidiurnal constituents in the northwest and southeast ends and a single point for diurnal constituents in the center of the PG, near Bahrain (Bosch van Drakestein, 2014; Hyder et al., 2013; Ranaee et al., 2012; Reynolds, 1993).

#### **1.1.4 General circulation**

The circulation in the PG is driven by five types of forcing phenomena: wind-stress, surface buoyancy fluxes, freshwater runoff, water exchange through the Strait of Hormuz and tides (Thoppil and Hogan, 2010a). Observations of the water properties and circulation in the PG are limited in temporal and spatial coverage (Yao, 2008). There are only a few published basin-wide measurements:

- 1. Summer cruise by the German ship Meteor in 1948 (Emery, 1956).
- 2. Wintertime expedition of the Atlantis from Woods Hole Oceanographic Institution in 1976 (Brewer and Dyrssen, 1985).
- 3. The Mt. Mitchell expedition (Reynolds, 1993) on surveys in February and June 1992.
- 4. Compiling the available hydrographic data to describe the aspects of the seasonal variability (from January to August) of the water properties in the PG (Swift and Bower, 2003).
- Conducting measurements of the water exchange in the Strait, consisting of a mooring site in the deep channel in Strait and four seasonal transects across the Strait (Johns et al., 2003).

These measurements provide a long-term observation of the exchange process in the Strait. The Indian Ocean Surface Water (denoted IOSW) entering the PG through the northern part of the Strait is swerved along the Iranian coast and appears to form a basin-wide cyclonic circulation in the southern PG (Brewer and Dyrssen, 1985; Emery, 1956; Reynolds, 1993; Swift and Bower, 2003). Meanwhile, the relatively low salinity IOSW experiences a salinity increase and is converted into high salinity waters in the northern gulf and in the shallow southern gulf. A salinity front extending from the Strait separates the modified IOSW from the salty water in the PG. The intruding IOSW shows distinct seasonal variability, spreading much farther into the northern and southern gulf in early summer than in winter (Figure 2). There are two down-wind coastal currents on both the Arabian and Iranian coasts in the northern gulf. The densest waters are formed in the northern gulf during winter and propagate southward toward the Strait throughout the year (Swift and Bower, 2003). Slightly

less dense, though saltier, waters are formed on the shallow southeastern shelves, which spill more intermittently into the deep PG (Yao, 2008).



Figure 2: Schematic of the surface circulation in the PG expounded in Reynolds (1993). The dashed lines in the central part of the PG indicate the approximate seasonal location of the water mass front between fresh water of the Gulf of Oman and the more saline water of the PG.

Constricting the water exchange between the PG and the open ocean, the Strait of Hormuz plays a crucial role in determining the circulation in the PG. Observations in the Strait (Johns et al., 2003) suggest a three-component water exchange structure which contains:

- 1. A relatively fresh surface inflow of IOSW on the northern side of the Strait.
- 2. A saline deep outflow of the PG water in the southern part of the Strait.
- 3. A mean surface outflow of intermediate salinity at the southern side of the Strait which varies seasonally, including a relatively fresh inflow in spring.

#### **1.2 Model Description**

If not cited otherwise in the text, the information is summarized from (Backhaus, 2008, 1985, 1983; Backhaus et al., 2008) and Script of "Introduction to Modelling of Ocean Physics" from Prof. Dr. Jan Backhaus in University of Hamburg (See Appendix).

#### 1.2.1 VOM and HAMSOM

Topography is probably the most noticeable disturbance in ocean dynamics and yet still under-represented in ocean models. The 'quality' of ocean models is often measured by their horizontal resolution, rarely by their vertical. Some ocean regions would require higher resolution than others. Thus, it seems plausible and reasonable to place resolution where it is needed. This formed the start point for the development of vector- ocean-model (VOM), which utilizes a static vertical adaptive grid in z-coordinates to improve the approximation of both topography and flow by an increased vertical resolution at topographic boundaries. VOM emerged from HAMSOM (HAMburg Shelf-Ocean Model), a three-dimensional semiimplicit non-linear primitive equation model with a free surface (Backhaus, 2008, 1985, 1983).

Grids are organized in one dimensional vector containing only wet cells and being defined on z-coordinate. This explains the first part of the model's name (Vector). The grid generator operates separately from a routine that produces the vector indexing and other grid data needed by the model. Thus, the generation of grids for a given topography can be done in isolation from model specific issues. VOM is defined in a C-grid (Arakawa and Lamb, 1977) because it is most commonly and most successfully used for shelf ocean modelling (Backhaus, 1983). The adaptive grid generator delivers grids that can be implemented in any horizontal Arakawa-grid. An index-vector for the sea surface, i.e. for the 2D model domain is obtained by scanning the topography matrix while counting wet cells only, and storing their counts in the vector. The last vector element is a dummy that represents all dry cells that were discarded. For the approximation of closed boundaries in VOM, a pre-processing routine converts grid-data into an indexing and into wet/dry masks that comply with a C-grid. The vector-pointer that addresses the eight elements around a center-cell would deliver the (one) dummy-index for all dry neighbor cells. Velocity components with this index would be zero. In addition to dummy cells, individual wet/dry masks for scalars and vector-components are derived from the gridding data. They assure a correct treatment of properties and flow vectors at closed boundaries in any complex topography. This is exemplified by the implementation of an adjustable slip condition for coastal parallel flow in a C-grid at a meridional coast.

VOM inherited large and well-approved parts of the numerical scheme of HAMSOM (HAMburg Shelf Ocean Model) (Backhaus, 1985, 1983). HAMSOM served in regional seas studies, in support of environmental, ecological and fisheries studies for both shelf and ocean, and in regional climate investigations (Backhaus, 1996; Backhaus et al., 2008; Hainbucher

and Backhaus, 1999; Harms et al., 2000; Huang et al., 1999; Janssen et al., 2001; Schrum and Backhaus, 1999; Stronach et al., 1993).

The numerical scheme of VOM has two important backbones inherited from HAMSOM (Backhaus, 1983). One is the implicit solution of the heat conduction equation in the vertical, here extended to also include advection. In view of the variety of vertical grid sizes in adaptive grids in VOM\_sw3d, this is a necessary pre-requisite for numerical stability. The other is the implicit solution of the free surface problem, which allows avoiding time splitting. That is, internal and external dynamics are always coupled. Time splitting, when considering a shelf-ocean exchange, for instance, could cause a problem for relevant time scales of deep and shallow regions may differ. VOM being designed to encompass oceans and coastal seas with a locally isotropic vertical resolution therefore deliberately avoids a time splitting (Backhaus et al., 2008).

Implicit schemes in VOM follow the classical approach (1) of Crank and Nicholson (1947) but are applied in a slightly different form with the intention to increase the scheme's accuracy by predicting temporal changes of properties rather than properties.

$$\boldsymbol{\phi}^{n+1} - \boldsymbol{\phi}^n = \Delta t \left( \alpha L(\boldsymbol{\phi}^{n+1}) + (1-\alpha)L(\boldsymbol{\phi}^n) \right)$$
(1)

Here  $\boldsymbol{\alpha}$  is the Crank–Nicholsen (CN) 'implicitness' pointer [0, 1], and n denotes the timelevel. L is a spatial difference operator applied to the property to be predicted  $\boldsymbol{\phi}$ .  $\Delta t$  is the time step. The definition of:  $\boldsymbol{\phi}^{n+1} = \boldsymbol{\phi}^n + \Delta \boldsymbol{\phi}^{n+1}$  is used, where  $\Delta \boldsymbol{\phi}^{n+1}$  is the temporal change of  $\boldsymbol{\phi}$  within one time step. This allows implementing  $\Delta \boldsymbol{\phi}^{n+1}$  as the prognostic property of the implicit scheme. Replacing  $\boldsymbol{\phi}^{n+1}$  in (1) by the above definition we arrive at the implicit scheme (2) utilised in VOM for predicting temporal changes of properties

$$\Delta \boldsymbol{\phi}^{n+1} = \Delta t \left( \alpha L(\boldsymbol{\phi}^{n+1}) + L(\boldsymbol{\phi}^n) \right)$$

In Crank and Nicholson (1947) a pointer  $\alpha$ =0.5 was used, which ensures a neutrally stable scheme void of amplitude damping. Apparently, with  $\alpha$ =0, the scheme would degenerate to an explicit one.

The procedure for solving a time step in VOM relies on the philosophy that all components are solved individually and independently and that their sum yields the final result. A 'component' could be one or more terms in the governing equations. The heat conduction equation, for instance, is treated as one component, and each component has its own subroutine. Therefore, the code of VOM is strictly modular.

#### 1.2.2 VOM-SW2D and 3D

The Vector Ocean Model Shallow Water 2d (VOM-SW2d) is a two dimensional semiimplicit nonlinear model which is developed at the institute of oceanography at the university of Hamburg. It emanates from HAMSOM (Alvarez Fanjul et al., 1997; Backhaus, 1985) and VOM. The model has new advection schemes implemented and allows for flooding and drying of individual grid cells.

VOM-SW2d (Backhaus, 2008; Backhaus et al., 2008) has a two-dimensional numerical scheme in a horizontal plane approximates the vertically integrated primitive shallow water equations in a rotational framework. These also called 'storm-surge' models are central components of three-dimensional ocean models for they deliver the spatial and temporal evolution of the free surface, and thus an integral part of the pressure field. It is two-dimensional primitive equation model by including rotation, diffusion, advection of momentum, and passive tracers to mark the flow. The model is capable to operate in an arbitrary topography with islands etc. Rotation is approximated in the presence of an irregular coastline. The same applies for the approximation of lateral momentum diffusion controlled by a slip boundary condition. More details in each case of this study have explained in the chapters.

VOM\_sw2d is a model in vector-notation (VOM: Vector-Ocean-Model); sw2d stands for 2D in shallow water. That is, the computational domain is mapped onto a one-dimensional 'wet-only' vector leaving out all cells covered by land, yet including any cells that potentially may be wetted. The model incorporates a wetting algorithm (Backhaus, 1976) which in the past has been optimized for many applications. It allows simulating wetting and drying of low-lying coastal areas. Non-linearity in the model stems from the equation of continuity (momentum in divergence), seabed friction, and the non-linear advective terms which numerically are approximated by a Lagrangian Upstream Scheme. For parallelization, the VOM-vector is chopped into N partitions, where N is the number of available computational nodes. Each node runs with a performance close to 100% because the vector only contains wet cells.

# Chapter 2

The results of this chapter have been already published in (Mashayekh Poul et al., 2016) and (Mashayekh Poul et al., 2014).

#### 2 The PG Tide Model

The main semidiurnal (M2 and S2) and diurnal (K1 and O1) tidal constituents are simulated in the PG. The topography is discretized on a spherical grid with a resolution of 30 seconds in both latitude and longitude. It includes coastal areas prone to flooding. The model permits flooding of drying banks up to 5 meters above mean sea level. At the open boundary, it is forced by 13 harmonic constituents extracted from a global tidal model. The Model results are in good agreement with tide gauge observations. Co-tidal charts and flow extremes are presented for each tidal constituent. The co-tidal charts show two amphidromic points for semidiurnal and one for diurnal tidal constituents. Maximum amplitudes of sea level are obtained for the north-western part of the PG, where coastal flooding prevails in wide areas. Strong tidal currents occur in different parts of the PG for each type of constituents. Maximum velocities are found in shallow regions. Particularly high amplitudes of elevations and high speed currents are founded in the canal between Qeshm Island and the mainland. Rectification of tides around Qeshm Island affects the propagation of tides in the PG as far as the coast of Saudi Arabia and the northern part of the PG.

#### 2.1 Setup and Forcing Data

The accuracy of regional tide models is often limited by bottom topography errors in particular in shallow regions (Quaresma and Pichon, 2013). The model topography for the PG, used in this study, has a horizontal resolution of 30 seconds (i.e. half a nautical mile) with a lateral open boundary on the east side of the domain. The data are provided by the

General Bathymetric Chart of the oceans from the British Oceanographic Data Centre (BODC). It is generated by combining quality-controlled ship depth soundings with interpolation between sounding points guided by satellite derived gravity data. However, this source reveals some missing topographic details along its continental slope and coast lines. To overcome this problem, manual adaptations have been done by incorporating satellite pictures and admiralty charts (Figure 3).



Figure 3: The topography of the PG (colorbar in meter), provided from data source GEBCO\_08 Grid version 20100927, by the General Bathymetric Chart of the oceans from the British Oceanographic Data Centre.

The model domain spreads meridionally from 23.6N to 30.6N and zonally from 47.5E to 57.3E. The average depth of the discretized topography in this study is 33.8m. The time step limited by the Courant-Friedrichs-Lowy criterion would be around 12 seconds. This criterion accounts for shallow water gravity waves and for the maximum depth occurring in this area. But the implicit free surface scheme in SW2d allows for a larger overall time step to reduce computational demands. A time-step of 15 seconds is used here.

The quadratic function of the barotropic current formulated for the bottom stress is parameterized by a bottom friction coefficient of 1.1e-3. For momentum diffusion, horizontal diffusion coefficients are calculated using Smagorinsky's Algorithm for each time-step from the velocity field.

13 principal constituents, including semidiurnal and diurnal tides, are extracted using the OSU Tidal Inversion Software (Egbert and Erofeeva, 2002) to be assembled and forced at the lateral open boundary. These harmonic constants are essential to reproduce the regional propagation of tidal waves, allowing non-linear harmonic interactions (Quaresma and Pichon, 2013). To account for realistic tidal elevations at the open boundary, the time-dependent astronomical variable of  $V_0+V$  was added to the surface elevation for phase correction.

The Model initialized from first of January 2011 and it simulated 12 consecutive months. Tidal harmonic constants were extracted using Tidal Analysis Toolbox (Pawlowicz et al., 2002) from the simulated surface elevation time series. The Tidal Analysis Toolbox uses harmonic analysis to estimate tidal constituents and their uncertainties in scalar and vector time series. Furthermore, tidal harmonic constants were extracted for 25 stations in the PG to validate the model results.

#### 2.2 Model Evaluation

There are two sources of observations in this study with totally 25 stations (Table 1 and Figure 4). For the observation from the Iranian National Cartographic Center, Harmonic constants for more than 40 tidal constituents are extracted from sea surface elevation time series of 2011 at 4 stations and sorted by amplitude. The first six constituents are shown here (Table 2). The temporal Resolution of the time series is 15 seconds for the model results and it is 30 minutes for the observations. Also, for the observation from the International Hydrographic office, 21 tidal gauges has used and first three constituents in ranges are used for comparison. In addition, comparisons plot the amplitude and phase of the model results and the observations are shown here (Figures 5 and 6). There is a good agreement in phases between model and observations. Maximum differences for amplitudes are in Bushehr station for K1 and P1, Khark station for M2, Kangan station for M2 and S2 and Emam-Hasan station for M2.

Nr.	Name	Nr.	Name	Nr.	Name	Nr.	Name	Nr.	Name
1	Bushehr	6	Khor Khwair	11	Zarqa	16	Mina al Ahmadi	21	Bandar Lengeh
2	Emam hasan	7	Ajman	12	Ras Laffan	17	Shatt al Arab	22	Jezirat Tunbh
3	Kangan	8	Dubai	13	Jabal Fuwairat	18	Asalu	23	Henjam
4	Khark	9	Khor Ghanada	14	Khwar Fasht	19	Jezirat Lavan	24	Bandar Abbas
5	Ras Dillah	10	H. al Mubarras	15	Ras al Mishaab	20	Jezirat Forur	25	Pasni

Table 1: List of tide gauges used if Figures 5. First 4 stations are provided by Iranian National Cartographic Center and others are provided by International Hydrographic Office.

These discrepancies in the model results arise most likely from deficiencies of the coastal topography, all around the domain. Moreover, some of the tide gauges like Bushehr station and Emam-Hasan station are located near port constructions which have topographic effects that cannot be resolved even by the high resolution used here. Also, the open boundary forcing is not perfect since it is created by another model. The harmonic constants, extracted from the OTIS regional tidal solution, of six tidal constituents at Khark station has been compared to the observations. Tidal constituents extracted from OTIS have used to prescribe tidal elevation at the open boundary. In this case, phases again fit better to observations compared to amplitudes (Figure 7).



Figure 4: Bathymetry of the region of PG. The numbers with white background indicate the location of tidal gauges listed in table 1. Data of red bullet locations is provided by Iranian National Cartographic Center and

	Model		Observation		Moo	lel	Observation		
	Amplitude (cm)	Phase (Degree)	Amplitude (cm)	Phase (Degree)	Amplitude (cm)	Phase (Degree)	Amplitude (cm)	Phase (Degree)	
		Μ	[2		K1				
Bushehr	36.67	132.67	36.74	123.91	24.81	234.1	33.05	230.22	
Khark	35.27	158.62	27.06	145.7	31.65	239.71	32.68	242.47	
Kangan	47.85	29.13	54.28	15.34	21.52	127.7	21.94	123.93	
Emam Hasan	52.73	177.21	45.02	168.73	35.91	240.66	35.92	235.68	
		S	2		01				
Bushehr	13.61	181.45	14.57	173.23	19.85	200.55	21.34	183.92	
Khark	12.07	205.17	11.09	200.55	23.55	207.25	20.86	197.08	
Kangan	15.16	71.79	19.9	56.79	13.58	105.47	11.72	88.4	
Emam Hasan	17.88	226.93	16.94	213.65	26.14	208.17	24.07	195.57	
		N	2		P1				
Bushehr	8.56	97.35	8.28	106.98	7.09	237.5	10.94	237.29	
Khark	8.41	130.38	9.11	131.08	10.47	246.78	10.81	249.54	
Kangan	12.01	0.76	12.48	13.91	7.12	134.77	7.26	131	
Emam Hasan	12.44	147.46	11.97	150.18	11.88	247.73	13.49	242.75	

blue is provided by International Hydrographic Office. The numbers with yellow background indicate the depth of contours in meters.

Table 2: Comparison between Model and Observation for tidal constituents of M2, K1, S2, O1, N2 and P1 in the PG. Phases are in degrees from Greenwich.



Figure 5: Comparison of Model and Observation for harmonics constants for M2, K1, and S2 in the PG.



Figure 6: Comparison of Model and Observation for tidal constituents of O1, N2, and P1 in the PG.



Figure 7: Comparison between, the OTIS regional tidal solution and Observation for 8 harmonic constants in the PG, obtained by harmonic analysis of the data provided by Iranian National Cartographic Center.

#### 2.3 Tide in the PG

Model results presented here include Co-tidal charts and flow extremes currents for each tidal constituent. The co-tidal charts show two amphidromic points for semidiurnal and one for diurnal tidal constituents. An amphidromic point is a point where the tidal fluctuation is

almost zero for one constituent and its occurrence hinges on the interference between Coriolis and bathymetry effects (Badri and Wilders, 2012). For other locations Diurnal, Semidiurnal or Mixed tidal cycles may dominate. In such cases, there is a factor to find the type of tide, named F-factor (Figure 8). Looking at the co-amplitude charts, the maximum and minimum points are exactly at the amphidromic points of two different constituents. The dominant tide is semidiurnal around the single amphidromic point of diurnal constituents and the dominant tide is diurnal around the amphidromic points of semidiurnal constituents.



Figure 8: Model Result for factor F over the PG.



Figure 9: Model Result for M2 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers



Figure 10: Model Result for K1 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers



Figure 11: Model Result for S2 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers.



Figure 12: Model Result for O1 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers.



Figure 13: Model Result for M2 maximum velocities over the PG in m/s.



Figure 14: Model Result for K1 maximum velocities over the PG in m/s.

The semidiurnal co-amplitudes of M2 and S2 constituents are very similar in shape but not in range, with M2 showing amplitudes almost larger by a factor of 2 than S2 (Figures 9 and 11). The tidal amplitude emerging from the Gulf of Oman decreases in southwesterly direction while passing through the Strait of Hormuz. Highest amplitudes, caused by wave trapping, occur between Qeshm Island and the Iranian mainland. The tidal wave propagates along the Iranian coast through the deeper part of the PG in westerly to northwesterly direction. It splits into two waves with an anti-clockwise sense of rotation, forming two amphidromic points in the Gulf. This is seen by a circular amplitude depression to the east of Qatar and north of United Arab Emirates. The second amphidromic point lies in the northern basin of the Gulf.

The semidiurnal tides in the Gulf form a bi-modal pattern of amphidromics with an anticlockwise sense of rotation, as confirmed by last studies (Al-Subhi, 2010; John, 1992; Lewis et al., 1968; Reynolds, 1993). For M2 and S2, the model reproduces the large amplitudes in the appropriate areas. For M2, these areas are the Qeshm canal and the region north of Gulf with amplitudes in the order of 110 cm, and the southeastern part of the Gulf in two sides of the amphidromic point in the order of 70 cm. For S2, the locations are similar but the amplitudes are in the order of 60 and 40 cm, respectively.

The diurnal Co-amplitudes of O1 and K1 constituents are similar in range (Figures 10 and 12) and also in shape, except the area near the Strait of Hormuz inside the PG. For O1, the tidal amplitude emerging from the Gulf of Oman increases in southwesterly and northwesterly direction while passing through the Strait of Hormuz. The tidal wave progresses along the Iranian coast through the deeper part of the Gulf in westerly to northwesterly direction. It splits into two waves with an anti-clockwise sense of rotation forming one amphidromic point in the Gulf. This is seen by a circular amplitude depression to the north of Qatar. For K1, the shape of propagation is nearly the same apart from the Strait of Hormuz. The tidal amplitude emerging from the Gulf of Oman decreases southward to the northern part of United Arab Emirates and increases in southwesterly direction while passing through the Strait of Hormuz. The model results suggest that diurnal tides in the PG form a single amphidromic point with an anti-clockwise sense of rotation as confirmed by (Al-Subhi, 2010; John, 1992; Lewis et al., 1968; Reynolds, 1993). The largest ranges of diurnal constituents occur at the head of the Gulf and along the coast of Saudi Arabia, the United Arab Emirates and Qatar.



Figure 15: Model result for M2 tidal ellipses in the PG. Blue ellipses rotate clockwise and red ellipses rotate anticlockwise.



Figure 16: Model result for K1 tidal ellipses in the PG. Blue ellipses rotate clockwise and red ellipses rotate anticlockwise.

The spatial distributions of the tidal ellipses of the different semidiurnal constituents, produced by the model results, are so similar that only those of the M2 ellipses are presented here for the first time (Figure 15). The same is valid for the diurnal ellipses and only the distributions of the K1 Tidal ellipses are given (Figure 16). The K1 tidal ellipse rotation is not always in the same direction as for M2 in the PG. In some areas, M2 constituent ellipses rotate cyclonic while K1 is anticyclonic. They have mostly elongated shape. The shape of ellipses can be important in the case of energy because of the time that turbines can turn with minimum velocity needed (Mashayekh Poul et al., 2014).

Tidal currents can be fast nearly everywhere in the Gulf and they do not depend on the type of tide (Pous et al., 2013). To provide comprehensive overviews of the magnitude of tidal currents, maximum current speeds in the PG over one tidal period are illustrated here (Figures 13 and 14). The figures show the maximum current speed for two runs with a single harmonic constant at the open boundary. These currents are not necessarily fully developed at the same time everywhere.

The spatial distributions of the tidal currents of the different semidiurnal constituents are so similar that only those of the M2 ellipses are presented here. The same is valid for the diurnal tidal currents and only the distribution of the K1 Tidal currents is given. The maximum velocity of M2 and S2 constituents are very similar in shape, but not in range, with M2 velocities almost twice as large as S2 velocities, similar to the amplitudes. For the O1 and K1 constituents, both shape and range are similar, except in the Strait of Hormuz. For semidiurnal tides, tidal currents are generally low along the PG. However, stronger semidiurnal currents are simulated for the northern head of the Gulf and Qeshm canal.

Currents are also locally strong in limited areas around the islands, as confirmed by (Pous et al., 2013). Besides, Diurnal tides induce extreme current speeds in four areas: the Strait of Hormuz, the northern head of the Gulf at the entrance of Musa estuary, north of Qatar and Qeshm canal. Tidal currents for K1 are much stronger than for O1 in the Strait of Hormuz. Semidiurnal tides induce extreme currents in two areas: the northern head of the Gulf at the entrance of Musa estuary and Qeshm canal.

Because of high resolution in topography as compared to other studies in the PG (Bosch van Drakestein, 2014; Ganj, 2013; Gorji-Bandpy et al., 2013; Pous et al., 2013; Sabbagh-Yazdi et al., 2007), both diurnal and semidiurnal tides induce high amplitudes and extreme current speeds (more than 2 m/s) in Qeshm canal.

#### 2.4 Kinetic energy

The tidal stream energy can be calculated by the kinetic power density from the tidal current (Figure 18) as (Bahaj and Myers, 2004; Chen et al., 2013; Nicholls-Lee, 2011):

$$P=\frac{1}{2}C_t\rho U^3$$

where P is the tidal stream power per unit area;  $C_t$  is the turbine efficient coefficient, represents the effectiveness of a device in generating power, regardless of flow speed or capture area of the device.  $\rho$  is the density of sea water; and U is the speed of the tidal current. To designate areas suitable for tidal energy conversion the summation of all tides is essential (Figure 17).



Figure 17: Maximum tidal currents velocity (colorbar in m/s) in the PG using 13 tidal constituents at the open boundary.



Figure 18: Kinetic power density (colorbar in kW/m<sup>2</sup>) from the tidal current.

On the other hand, for energy conversion not only the magnitude but also the duration of currents must be considered. The result reveals that the highest power density exceeded 18 kW/m2 in the entrance of Musa estuary. Also, it reveals that there is high power density area along the Qeshm canal and around the islands. However, to find the appropriate region for the deployment of tidal turbines more geological study is needed. As a suggestion, regions around the entrance of Musa estuary, Qeshm canal and islands in the PG with deep and flat bathymetry have high power density for tidal stream power generation.

To have estimation about the annual kinetic energy output, averages of 1.71 kW/m2 and 1.46 kW/m2 are calculated for the entrance of Musa estuary and Qeshm canal. The annual energy output would be 14.979 MW/m2 and 12.789 MW/m2 per turbine. Considering a diameter of 11 m and the swept area of 95.03 m2 for a turbine (Chen et al., 2013), the annual energy output would be 1423 MWh and 1215 MWh per turbine. If 50 turbines are deployed in one row, the total tidal energy would be 71.1 GWh and 60.7 GWh per year.

#### 2.5 Effect of Qeshm Canal

Wave trapping at the western part of the Qeshm canal occurs because of the phase difference and sea level gradient between the western and center part of the canal. The phase

difference arises from the narrow part of the canal at its center. Model results from 4 different tests show the effect of Qeshm Island in the propagation and magnitude of tides. In the first test, model resolved the normal topography of the PG and shows the range of the constituents. In the second test, Qeshm canal was closed on the western side and for the next test, the closed part was located at the center, which is the narrowest part of the canal. For the last test, both sides of the canal were closed. M2 and K1 have chosen for the tests as samples for semidiurnal and diurnal tides.

For K1, the result shows the negligible difference between closed and open canals, a maximum of 1cm in range. But for M2 the difference is considerable. In this case, the maximum difference between the normal and closed canal is around 10cm of the range (Figure 19). Maximum differences are in the last test and occur in the northern part of PG, north of Qatar, both on the Iranian side and the coast of Qatar. There is also a difference of around 5cm along the coast of Saudi Arabia. Unfortunately, the models with low resolution cannot resolve this area and this error is always in their result.



Figure 19: Effect of Qeshm canal on the tidal solution with single harmonic forcing (M2) at the open Boundary, Model Result for tidal range difference of M2 amplitude in two conditions; closed canal and real topography in cm (real-closed).

# Chapter 3

The results of this chapter are presented in a paper in revision in JGR.

#### **3** The PG Tidal Residual Currents

#### **3.1** Topography and circulation in the PG

As described in the first chapter, the PG is a shallow semi-enclosed marginal sea between Iran in the north and the Arabian Peninsula in the south. It is connected with the Gulf of Oman and the Indian Ocean through the Strait of Hormuz. The length of the PG is about 1000 km in Northwest to Southeast orientation; the width varies from a maximum of 338 km to a minimum of 56 km in the Strait of Hormuz, as reported in other studies in this area (Chao et al., 1992; Chu et al., 2008; Moeini et al., 2010; Reynolds, 1993; Yao, 2008). As the PG is located between the Arabian Plate and the Iranian (Eurasian) Plate, topography features in the northern and southern PG are different. The coastal topography bordering the PG shows distinct contrast; while the Iranian coast is mountainous, the Arabian coast is mostly a desert plain except close to the Strait of Hormuz.

The topography of the PG is dominated by soft sediments. It is generally deeper near the Iranian coast and is deepest near the opening of the Strait of Hormuz. The average depth of the topography is about 35-36m (Badri and Wilders, 2012; Moeini et al., 2010; Ranaee et al., 2011; Reynolds, 1993; Thoppil and Hogan, 2010a). This basin has a relatively shallow zone near the closed end of it, extending all the way along the southern part of the basin, roughly connected to one deeper part, with a clearly asymmetric cross-sectional depth profile of the main part. The maximum depth in the deeper part is 80 m while in the Straits of Hormuz depths can exceed 100 m (Pous et al., 2004a; Roos and Schuttelaars, 2010).

As described in section 1.1.1, the coastal boundary and the bottom topography of the PG are very irregular and several islands of various sizes and shapes are spread over the region (Sabbagh-Yazdi et al., 2007). From geological studies in this area (Edgell, 1991; Perotti et al.,

2011; Sarnthein, 1972; Seni and Jackson, 1984; Thomas et al., 2015; Zaigham et al., 2013), in the southern basin of the PG there are numerous salt domes with circular shape, while in the Northern Basin they mostly have an elliptical shape and are connected by elongated ridges. Holocene sediments in the PG are primarily carbonates. Shallow domes form mounds on the seafloor, and particularly active diapirs form islands exposing salt at the surface (Kent, 1979; Purser, 1973). Under marine conditions, sand can accumulate by winnowing on bathymetric shoals. Consequently, Salt domes having sufficient surface expression are overlain by sand-rich sediments. Small reefs might also be expected on topographic highs over dome crests. Such dome crest reefs have been recognized in the PG (Purser, 1973; Seni and Jackson, 1984).

Purser in 1973 subdivided bathymetric highs in the PG. Based on his approach bathymetric highs in the PG have been grouped into three classes based on their setting: outer, intermediate and inner.

- 1. The central parts of the basin are characterized by numerous highs with marked vertical relief.
- 2. The sloping sea floor is characterized by a great variety of highs and depressions.
- 3. Highs situated close to the mainland shoreline may considerably affect coastal sedimentation.

In most continental shelf seas, such as the PG, the highest current speeds are associated with the barotropic tides. In general, tides in the PG are complex. The dominant tidal pattern changes from primarily semidiurnal to diurnal (Mashayekh Poul et al., 2016; Pous et al., 2013; Reynolds, 1993). Barotropic tidal currents are described in detail in other studies (Mashayekh Poul et al., 2016; Pous et al., 2013). Tidal current speeds for M2 are in the range of 0.3 m/s to 1.0 m/s with maximum of 2.5 m/s in Qeshm Canal and for S2, O1 and K1 tidal current speeds are in the range of 0.2 m/s to 0.5 m/s (Mashayekh Poul et al., 2016).

In spring and summer, the wind stress generates south- eastern surface currents of the magnitude of about 0.05 m/s along the Saudi and Iranian coast. In addition, both the wind stress and heat fluxes cause the southward currents with speeds of 0.05–0.1 m/s from the Hormuz Strait and main basin of Gulf toward the UAE coast and Bahrain–Qatar shelf. In winter and autumn, the cooling effect of the thermohaline fluxes leads to a removal of the thermal stratification and density contrast between the surface and bottom waters. As a result, the vertical stability of water column weakens significantly and the baroclinic eddies with diameters of about 40–70 km and speeds of about 0.08– 0.15 m/s form in some parts of the
Gulf. In addition, the wind stress leads to shear instability and produce eddies with diameters of 30–120 km and speeds 0.04–0.15 m/s in most parts of the PG (Hosseinibalam et al., 2011).

Previous studies reported that the tidal residual flow influence on the overall circulation in the PG is minimal (less than 0.02 m/s) (Pous et al., 2013), except in a few localized areas (e.g., the Iranian coast and the Strait of Hormuz) where the tidal residuals are large enough to enhance the dominant density-driven flow (Thoppil and Hogan, 2010b). There are many other studies on wind and density driven circulation (Chao et al., 1992; Ezam et al., 2010; Hosseinibalam et al., 2011; Pous et al., 2015; Reynolds, 1993; Swift and Bower, 2003; Thoppil and Hogan, 2010a, 2010b); this chapter reviews only tidal residual currents.

## 3.2 Residual flow

Tidal Residual currents can be induced by mean sea-level slopes or nonlinearities of the dynamics of tidal flow. In tidal dynamics, nonlinear interactions of tidal flow with the bottom topography are represented by the advection terms of the momentum equations. These interactions are more important in areas where the tidal excursion is comparable to the scale of bathymetric features and around shallow points and capes (Lavín and Marinone, 2003). Numerical models are suitable to investigate the generation of shallow water currents and tidal residual flows as they can resolve the nonlinear processes (Davies and Jones, 1996; Dworak and Gómez-Valdés, 2003; Le Provost and Fornerino, 1985; Westerink et al., 1989). Also, shallow water tides can create residual currents due to the asymmetry between the flooding and ebbing phases. This process determines the flow structure over shallow regions, especially along coastlines and sloping topographies. In nature, tidal residual currents are usually one or two orders of magnitude weaker than the tidal current velocities (Robinson, 1981).

One way to drive the residual flow is separating the oscillatory and the mean part of the current, which is common practice in wave-driven current modelling. The models which simulate nonlinear tidal dynamics usually describe the depth-averaged velocity as a function of time. Integration over the tidal cycle yields the residual current, in which the mass flux as well as tidal and bed shear stress effects are included (Bakker and de Vriend, 1995).

#### 3.3 Model Description and Methods

In this study, a two dimensional model (VOM\_sw2d) is used to investigate the interaction between tidal wave and experimental symmetric, elongated and tilted obstacles, i.e. hills and valleys to illustrate flow pattern of residual currents passing through them. Then, the model was applied to explore tide induced residual currents in PG with high resolution real topography. The topography data are provided from data source GEBCO\_08 Grid version 20100927, by the General Bathymetric Chart of the oceans from the British Oceanographic Data Centre [*IOC, IHO and BODC,* 2003]. The structure of the residual circulation in the PG is obtained by averaging the simulated horizontal momentum components, which includes the nonlinearity of interaction between tidal wave and topography, over H (Babu et al., 2005; Quirós et al., 1992; Yuxiang, 1988). H is the actual water depth:  $H = Depth + \zeta$  where  $\zeta$  is sea surface elevation.

$$u_{res} = \frac{\sum_{1}^{N} U}{\sum_{1}^{N} H}$$
, with a number of time steps  $N = T/dt$ 

Where  $u_{res}$  is residual velocity, U is momentum, T is the period of the tidal constituent and the time increment is dt. In the calculation T is 5 tidal periods to fit dt into the averaging period. The calculation is done after 20 periods of spin up to reach the stationarity of tidal wave propagation in the domain. This calculation is done for each tidal constituent separately.

The model domain spreads meridionally from 23.6N to 30.6N and zonally from 47.5E to 57.3E. It has a horizontal resolution of 30 seconds (i.e. half a nautical mile) with a lateral open boundary at the eastern end, representing the connection to the Indian Ocean. Each tidal constituent was applied separately in the forcing at the open boundary to the Oman Sea.

To demonstrate the shark-skin pattern of the PG seabed a high-pass filtered topography was obtained by subtracting the smoothed topography from the original one. The high pass filtered topography shows the existence of numerous hills and valleys in the PG-domain with scales well below the Rossby radius (Figure 20).



Figure 20: High-pass filtered topography of the PG in meters (colorbar). Box 1 indicates the area zoomed in Figure 28.

## 3.4 Results

## **3.4.1** Residual current in an experimental domain

In recent studies about tidal residual currents, it is mentioned that there is a relation between the slope of the bottom topography and residual current speeds (Carbajal and Backhaus, 1998; Dworak and Gómez-Valdés, 2003; Marinone, 1997; Quaresma and Pichon, 2013; Quirós et al., 1992; Zimmerman, 1978). To investigate the intricate interaction between tidal wave and bottom topography, a numerical experiment is constructed in an experimental domain (500 km, 1000 km). A channel created northward with a Dirichlet boundary condition at the southern boundary and a von Neumann boundary condition at the eastern, the western and the northern open boundary. Applying the model to the test channel illustrated flow patterns of residual currents passing through a symmetric, elongated and tilted obstacle, i.e. hill and valley.

Residual currents create four adjacent gyres around the symmetric hills and valleys with a symmetric flow field (Figure 21). For the case of a hill, going with the currents, there is a cyclonic gyre at the left side and an anti-cyclonic gyre at the right side before the hill and

opposite directions downstream the hill. For the case of a valley, the directions of residual currents are opposite (Figure 22). When elongating the hill or valley to the shape of an ellipse, residual currents are stronger along the major axis of the ellipse compared to the minor axis and the directions of residual currents are the same as for the symmetric case (Figure 23). In the case of an elongated and tilted hill or valley, two gyres along the major axis mix and create a long ellipse shaped gyre (Figure 24). From the experiment, a distinct residual current pattern is found due to the interaction between different types of hills and valleys (Figure 25).



Figure 21: Residual current ( $\times 10^{-3}$ m/s) pattern around a symmetric hill. The current direction of approach flow is northward. The background and vectors display the Residual currents. White contours are the topography contours.



Figure 22: Residual vorticity ( $\times 10^{-6}$  s<sup>-1</sup>) pattern around a symmetric hill (left) and a valley (right). The current direction of approach flow is northward.



Figure 23: Residual current (×10<sup>-3</sup>m/s) pattern around an elongated hill (left). The background and vectors display the Residual currents. White contours are the topography contours. Residual vorticity (×10<sup>-5</sup> s<sup>-1</sup>) pattern around a symmetric hill (right). The current direction of approach flow is northward.



Figure 24: Residual current (×10<sup>-3</sup>m/s) pattern around an elongated and tilted hill (left). The background and vectors display the Residual currents. White contours are the topography contours. The residual vorticity (×10<sup>-5</sup> s<sup>-1</sup>) pattern around an elongated and tilted hill (right). The current direction of approach flow is northward.



Figure 25: The residual current around a hill and a valley. Wide arrows are the current direction of approach flow. The background contours display the topography. For a hill, water depth decreases to the center and for a valley, it increases. Gyres illustrate the direction of residual current around the topography contours. Looking in the direction of the flow cyclonic and anticyclonic gyres are on different sides in the case of a hill and a valley.

## 3.4.2 Residual current in the PG

An average of the simulated flow over an integral number of diurnal (Figure 26) and semidiurnal (Figure 27) tidal cycles yields the residual circulation in PG. It is possible to see this pattern of residual current since high resolution topography with details caused by salt domes is used.

The residual current speeds have nearly the same spatial distribution of diurnal and semidiurnal constituents in the PG. This is in agreement with the theoretical explanation that the residual currents are due to nonlinear interactions of tidal flow with topography (Komen et al., 1981; Marinone, 1997; Quirós et al., 1992; Yuxiang, 1988; Zimmerman, 1978). However, the currents do not have the same strength in different areas and strong residual currents appear in different areas for each type of constituents. Based on the results of the experiment, beside the magnitude of tidal wave velocity, this might be because of the different flow direction for diurnal and semi diurnal tidal wave.

By applying the model to simulate tidal residual currents in the entire PG, a distinct residual current pattern is found due to the interaction between different types of hills and valleys. Diurnal tide-induced residual current velocities are strong in the north of Qatar and



Bahrain, the eastern coast of Qatar, the Strait of Hormuz and above the northern coast of Saudi Arabia, between Bahrain and Kuwait (Figure 3).

Figure 26: Model Result for K1 residual velocity (m/s) in the PG.



Figure 27: Model Result for M2 residual velocity (m/s) in the PG.

For semidiurnal residual currents, these areas are the Iranian coast on the western side of Qeshm Island, the eastern side of Qatar north of United Arab Emirates, around Bahrain, and the northern part of the PG. The total residual current has a speed of more than 0.02 m/s, 0.05 m/s and 0.1 m/s in 68.8%, 29.5% and 9.4% of the model domain. M2 has a maximum tidal residual velocity of more than 0.1 m/s around steep domes in the PG. It is 13.4% of maximum barotropic tidal current around Lavan Island. The other semidiurnal and diurnal tides have maxima of 0.05 m/s and are hence less important than M2.

By plotting high-pass filtered topography contours and M2 residual velocity vectors in one figure, the experiment is scrutinized in real topography (Figure 28). The figure indicates that velocity vectors tend to be normal to topography contours or flow patterns have a tendency to be proportional to the topographic slope (Huthnance, 1973; Maas et al., 1987).

An experiment using 3065 Lagrangian trajectories inside the PG indicates the presence of many adjacent gyres rotating in opposite directions. In fact, the entire PG is peppered with barotropic eddies. Inspecting the residual vorticity field (Figure 29), neighboring eddies turn in different direction and trajectories follow the coastline in the coastal area. The longest trajectory between start to end point is 223 km in 120 days in the northern PG. Certainly, there are more trajectories with a length greater than that, but they may not be important for the general circulation pattern because they always turn around with small radius in the same place. Two main cyclonic circulation patterns are found in the central part of the PG (Figure 30). The radius of the gyres increases with the distance from the entrance of the PG through the Strait of Hormuz. Only one of these gyres, to the north of Qatar, has been reported before (Pous et al., 2013). There is also a strong westward coastal current in the northern PG which continues southward to 28 N in Saudi Arabian coast and turns eastward again (Figure 29). In this area, residual current can exceed 0.15 m/s while the maximum barotropic tidal current is around 1.5 m/s.



Figure 28: M2 Residual current vectors around a hill in high-pass filtered topography (colorbar in meters) of the PG. vectors show the M2 residual currents. CD is the Current Direction. This area is shown in Figure 1 with Box 1.

The behavior of the tidal wave passing through a hill or a valley in different situations (Figure 25) and high-pass filtered topography (Figure 20) can explain the complicated system of gyres in PG. Finally, for a better illustration of the flow structure, the PG is divided into 3 boxes in which all tracer trajectories are shown (Figures 31, 32 and 33). Results reveal a very rich eddy field.



Figure 29: Lagrangian trajectories (black lines) in residual vorticity (colorbar  $\times 10^{-5}$  s<sup>-1</sup>), running with residual velocities of M2+S2+K1+O1 for 120 days.



Figure 30: Lagrangian trajectories (black lines) in residual vorticity (colorbar  $\times 10^{-5}$  s<sup>-1</sup>), running with residual velocities of M2+S2+K1+O1 for 120 days. Green lines show 2 main gyres in the PG. The red box in guide map shows the position of zoomed figure in the PG.



Tidal Residual Currents in The Persian Gulf

Figure 31: Box 1 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points.



Figure 32: Box 2 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points.



Figure 33: Box 3 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points.

## Chapter 4

### 4 Tidal Resonance in the PG

I investigated resonance in the PG by applying a non-linear hydrodynamic numerical tidal model to the PG. The model was used to characterize the amplified response of the basin to different forcing periods. It was forced with one and the same amplitude at its open boundary to the Oman Sea by waves with periods ranging from 3.5 h to 35.5 h with increments of 0.5 hours. Each wave was simulated separately. The results reveal that in three areas tidal elevations are significantly larger than the forcing amplitude indicating resonance. These are the northern PG (maximum Amplification Factor (AF) = 1.61), the Strait of Hormuz (maximum AF = 3.00), and the southern PG (maximum AF = 1.33). The amplification factor (AF) is defined by the ratio of local amplitudes vs. forcing amplitude. Diurnal tides are resonant in both northern and southern PG. Semidiurnal constituents are amplified in the northern Gulf as well as in the Strait of Hormuz. A simulated sea level rise due to climate change of 1 meter increased the AF off the Arabian coast for semidiurnal tides from 0.72 to 1.21. In the Qeshm Canal in the Strait of Hormuz, AF increased from 1.36 to 1.57 for semidiurnal and from 0.73 to 1.1 for diurnal tides.

### 4.1 The PG

The PG is a shallow semi-enclosed marginal sea between Iran and the Arabian Peninsula. It is connected with the Gulf of Oman and the Indian Ocean through the Strait of Hormuz. The length of the PG is about 1000 km in Northwest to Southeast orientation; the width varies from a minimum of 56 km in the Strait of Hormuz to a maximum of 338 km. The coastal topography bordering the PG shows distinct contrast; while the Iranian coast is mountainous, the Arabian coast is mostly a desert plain except close to the Strait of Hormuz.

The bottom topography of the PG is generally deeper near the Iranian coast (Figure 34.a). The deepest area is near the opening of the Strait of Hormuz. The average depth of the basin is about 35-36m (Badri and Wilders, 2012; Moeini et al., 2010; Ranaee et al., 2012; Reynolds, 1993; Thoppil and Hogan, 2010a). The basin has a shallow zone near the closed end in the north, which extends all the way along the Arabian Peninsula towards southern the part of the basin. The PG has a clearly asymmetric cross-sectional depth profile in its main part. The maximum depth in the deeper part is 80 m while in the Straits of Hormuz it exceeds 100 m (Pous et al., 2004a; Roos and Schuttelaars, 2010).



Figure 34: a) The topography of the PG, contour lines with an increment of 20 m. Y-axis: latitude; X-axis: longitude. b) Displacement of amphidromic points with different periods of forcing (10 h to 35 h), Blue circles: periods with 2 amphidromic points, Red circles: periods with a single amphidromic point. c) The position of monitoring stations; N1-N4 stations in the northern PG, S1-S4 stations in southern PG, H1-H4 stations in Strait of Hormuz. Data at monitoring stations are shown in Figures 39, 40 and 41.

Tides in the PG are complex (Mashayekh Poul et al., 2016; Pous et al., 2012). The dominant tidal pattern changes from being primarily semidiurnal to diurnal (Reynolds, 1993). The leading tidal constituents in this area are M2, K1, S2, O1, N2, and P1. This order may

change with the F-factor at other locations in the domain. The F-factor shows the type of tide between diurnal, semidiurnal, and mixed. It is defined as the ratio of the main diurnal over the main semidiurnal constituent's amplitudes. In the PG, it is K1+O1 for diurnal and M2+S2 for semidiurnal tides (Najafi, 1997).

The PG has a natural period of 22.6 or 21.7 hours for tidal waves based on the Japanese and Chrystal method (Defant, 1961). Semidiurnal and diurnal waves interact in the basin and form a system of amphidromic points of Kelvin-Taylor type (Pous et al., 2013). There are two points for semidiurnal constituents in the northwest and southeast, and a single point for diurnal constituents in the center of the Gulf, near Bahrain (Bosch van Drakestein, 2014; Hyder et al., 2013; Ranaee et al., 2012; Reynolds, 1993).

#### 4.2 Tidal Resonance

There are a number of coastal regions on earth the Eigen-oscillations of which being in resonance with the tide. The resonance is the amplified response of a basin to periodic forcing (Carbajal and Backhaus, 1998) close to its eigen-period. Resonant amplification is the ratio between the wave height at a location within the basin and that at the open boundary (Carbajal and Backhaus, 1998; Liang et al., 2014). The response of a basin to tidal forcing depends on the properties of offshore tides and the influence of friction (Sutherland et al., 2005). The most important parameters are the geometry of a basin, i.e. length, depth, dissipation, and amplitude of forcing (Backhaus, 2015; Skiba et al., 2013). In fact, resonance occurs when a forcing excites a natural mode of a system (Le Souëf and Allen, 2014).

Tidal waves behave similar to the long waves, and their wavelength exceeds the depth of water in which they exist. The wavelength for the tidal waves is given by  $\mathbf{L} = 2\pi \sqrt{gH}/\omega$ , where g is acceleration due to gravity (ms<sup>-2</sup>), H is the depth of water (m) and  $\omega$  is the angular frequency of the tidal component (radians s<sup>-1</sup>). Resonance in a tidal basin is most striking if the quarter wave-length criterion applies (Defant, 1961; Godin, 1993; Proudman, 1953). That is, if the length of the basin is about a quarter wavelength of the forcing oscillation. The resonance amplification of the tides at PG occurs due to the dimensions of the PG.

Blain (1998) reported resonant amplification of the semidiurnal and diurnal tides in the northern PG. Hyder et al. (2013) showed that the dimensions of the Gulf result in the resonant amplification of both the diurnal and semidiurnal tides. Roos and Schuttelaars (2010) stated that the PG has a tidal resonance associated with the topography near the basin's closed end.

A number of studies have argued that coastal regions around the globe are in resonance with semidiurnal or diurnal tidal forcing (Arbic et al., 2007; Backhaus, 2015; Garrett, 1972; Sutherland et al., 2005). Apart from cases with confirmed full and spectacular resonances, there may be other regions with only weak or latent resonance. The latter, however, remained largely understudied. The term 'latent resonance' should be understood as a not fully developed resonance i.e. juvenile resonance (Backhaus, 2015). In coastal regions, resonant or latent resonant responses add to the complexity of the tidal pattern and tend to intensify nonlinear effects (Andersen et al., 2006). However, knowing how close a system is to resonance provides an indication of the sensitivity of the local tidal regime to gradual changes in mean sea level and to changes in geometry caused by human activities (Sutherland et al., 2005). Using a numerical model, the frequency- dependent response of a coastal region can be determined.

## 4.3 Model Description

The characteristics of tidal resonance were investigated by using the vector ocean model shallow water (VOM-SW2d), a non-linear hydrodynamic tidal model, and applied it to the PG (Mashayekh Poul et al., 2016). The model domain spreads meridionally from 23.6 N to 30.6 N and zonally from 47.5 E to 57.3 E. It has a horizontal resolution of 30 seconds (i.e. half a nautical mile) with a lateral open boundary at the eastern end, representing the connection to the Indian Ocean. In this chapter, the resonance characteristic of the PG is presented based on the non-linear shallow water equations for periods ranging from 3.5 h to 35.5 h.

#### 4.4 Tidal resonance in the PG

To investigate the resonance characteristics of the PG, a numerical experiment is ascertained with 33 runs with different periods. The amplitude of the wave at the open boundary was maintained at 1 m, but the period of oscillation was varied. The periods of forcing ranged from 3.5 to 35.5 hours with a resolution of 30 minutes. For the 12.5 hours period (Figure 35), which is close to M2 tide, the shape of the tidal AF was similar to the tidal range of the M2 from recent studies (John, 1992; Reynolds, 1993). Two amphidromic points are found in the positions reported before (John, 1992; Mashayekh Poul et al., 2016; Pous et al., 2013; Reynolds, 1993). For the 24 hour period (Figure 36), which is close to K1 tide, the shape of the tidal AF and position of the single amphidromic point is in agreement

with previous studies (John, 1992; Mashayekh Poul et al., 2016; Pous et al., 2013; Reynolds, 1993).

Based on the results from 33 runs with different periods, propagation of waves is described in the PG. It was found that the system of the amphidromic points is related to the period of the tidal forcing (Figure 34b). As a result from the model, there are two amphidromic points in the period of 10 h to 21.5 h, and above the latter period, there was only one amphidromic point in the PG.



Figure 35: Tidal amplification factor (colorbar) for the period of 12.5 h in the PG. Y-axis: latitude; X-axis: longitude.



Figure 36: Tidal amplification factor (colorbar) for the period of 24 h in the PG. Y-axis: latitude; X-axis: longitude.



Figure 37: Periods (from 3.5 h to 35.5 h) of maximum tidal ranges in the PG. Y-axis: latitude; X-axis: longitude; Colorbar: Period in hours.



Figure 38: Maximum tidal amplification factor (colorbar) from period 3.5 h to 35.5 h in the PG. The neutral tidal amplification factor is shown by the contour. Y-axis: latitude; X-axis: longitude.

I determined the Periods of maximum tidal ranges in the PG (Figure 37) from the model results. This allows dividing the PG into 4 main sections. There is a sharp border between semidiurnal and diurnal tides for the periods of the maximum amplitude. These results agree with the shape of F-factor in the PG, which shows the dominant tide in that region (Najafi, 1997). Diurnal tides have a maximum amplitude in the northern PG and near the region off the Arabian coast. Semidiurnal constituents are also amplified in the northern Gulf and additionally in the Strait of Hormuz and in the area north of Qatar. In the center of the PG, there is a region of semidiurnal resonance that is embedded amongst regions with diurnal resonance.

Maximum tidal AF in the PG domain shows three areas with higher resonance (Figure 38). The northern PG, the Strait of Hormuz, and the southern PG are the main areas with pronounced resonance in the PG. The following areas also show resonant features: the southern and eastern part of Qatar, western side of the United Arab Emirates coast, and the region off the Saudi Arabia's coast between Qatar and the United Arab Emirates. In the northern part of Qatar, semidiurnal tides have maximum amplitudes as compared to diurnal. Figure 37 and Figure 38 clearly demonstrate the resonance characteristics of the PG.

I also scrutinized the variation of the sea surface elevation at different periods at 12 monitoring points serving as virtual tidal gauges. Figure 34.c shows Position of monitoring stations for the water surface variations over three high resonance regions; N: the northern PG, H: Strait of Hormuz and S: Arabian coast in the southern PG. A response curve for each monitoring point can then be constructed by plotting the AF versus the wave period. The curve shows the water level oscillation response to the excitation at the sea boundary at different frequencies. Each area is plotted in separate figures in order to distinguish the curves with different points (Figures 39, 40 and 41).

Two resonance peaks at ~13 h with AF ranging from 1.15 to 1.4 and at ~27 h with AF between 1.3 and 1.45 appear in the northern PG (Figure 39). There periods of resonant peaks lie in the range of diurnal and semidiurnal tidal constituents. Interestingly, both diurnal and semidiurnal tides are in resonance which explains why tidal ranges in the shallow, dissipative northern PG are much higher than elsewhere in the gulf. However, in the Strait of Hormuz diurnal and semidiurnal tides show signs of resonance.

There are two local peaks of resonance in the Strait of Hormuz (Figure 40). One of them at about 12.5 h with the AF between 0.9 and 1.35, and the other one at about 27 h with the AF between 0.8 and 1.1. The first peak is in the range of semidiurnal tides.



Figure 39: Tidal amplification factor for the monitoring points, N1-N4, in the northern PG (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines.



Figure 40: Tidal amplification factor for the monitoring points, H1-H4, in the Strait of Hormuz (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines.



Figure 41: Tidal amplification factor for the monitoring points, S1-S4, in the region off the Arabian coast (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines.

Two resonance peaks, one at ~15 h with the AF from 0.95 to 1.2, and the other one at~25 h with the AF from 1.1 to 1.3 can be observed in the region off the Arabian coast (Figure 41). In this area, diurnal tides are in resonance.

The change in the tidal range, over time, is one of the main contributions to the local processes (Hill et al., 2011). For example, sea level changes affect the width and bathymetric depths of the PG, and hence the reflection and amplification of tidal waves and the distribution of frictional dissipation of the tidal energy that is transferred from the Indian Ocean to this shallow regions. For any constructions at the sea level, it is crucial to understand the relationship between tidal levels and the sea level indicators. Recent studies have shown that the average sea level rise in the PG is about 0.33 m and 0.59 m under different climate change scenarios for the period of 2000-2100 (Goharnejad et al., 2013). The very low-angle geometry of the coastlines around the PG, mainly in the south, results that this region is extremely sensitive to fluctuations in sea level. Even small variation in sea level will result in significant lateral shifts in coastline (Lokier et al., 2015).



Figure 42: Increase of tidal amplification factor (colorbar) for the period of 12.5 h due to sea level rise of 1 m in the PG. Y-axis: latitude; X-axis: longitude.



Figure 43: Increase of tidal amplification factor (colorbar) for the period of 24 h due to sea level rise of 1 m in the PG. Y-axis: latitude; X-axis: longitude.

Further, a sea level rise may have an effect on tidal resonance. A numerical experiment is conducted to investigate the effect of climate change in which it is assumed a sea level rise of 1 m for the PG. AF for 2 periods are extracted, i.e. 12.5 h (Figure 42) for semidiurnal and 24 h (Figure 43) for diurnal oscillations. For semidiurnal tides, a maximum increase of 0.49 (68%) in AF is found in the region off the Arabian coast and 0.19 (14%) in the Qeshm Canal. For diurnal tides, AF in the Qeshm Canal increased by a factor of 0.35 (48%). Further the sea level rise caused a change in the position of the amphidromic points for semidiurnal and diurnal tidal periods.

## 4.5 Potential energy

High amplitudes of sea surface elevations suggest that tides can provide a great amount of potential energy in the PG. The results from a tidal model of the PG conclude that the tidal range increases significantly in the northern PG and Qeshm canal in Iranian side, as a result of resonance. With stronger demands for green energy and the development of new technology, the prospect of tidal power has resurfaced (McMillan and Lickley, 2008). In section 2.4 the kinetic power density has calculated from horizontal velocity field. Also, the area with the most efficiency of energy producing from the tidal stream has been marked. Here, the result reveals that the annual potential energy of semidiurnal tides exceeded 140

MW and 180 MW in the Musa estuary and Qeshm canal for a cell (~840 m\* 820 m) in the model domain (Figure 44). Diurnal tides have the maximum annual potential power around 22 MW in the region off the Arabian coast and in the Musa estuary for a cell area in the model domain (Figure 45). The maximum potential energy of semidiurnal tides (200 MW) is one order larger than the Maximum potential energy of diurnal tides (20 MW).



Figure 44: The annual potential power density (colorbar in MW/cell) of the semidiurnal tide.



Figure 45: The annual potential power density (colorbar in MW/cell) of the diurnal tide.

# Chapter 5

#### 5 High evaporation and inverse estuary of the PG

## 5.1 Musa estuary

Musa estuary is located in the north-west of the PG (Figure 46). The Imam Khomeini port, one of the chief ports of Iran, is located in the hearth of this estuary. Currents in the Musa estuary are formed due to tidal fluctuations in the PG as well as the complicated geometric features of this multi branch estuary (Sabbagh Yazdi and Sadeghi Gooya, 2010).

The climate in the Gulf region is arid, resulting in an excess of evaporation over precipitation plus river runoff. One of the results of evaporation from the sea surface in this area is the increase of salinity in the surface layer and in shallow tidal flats. Northwest winds bring interior continental air to cool the surface of the PG and heat loss from the sea surface is greatest at the northern end of the PG. So, the densest water forms there (Swift and Bower, 2003). In winter, higher wind speed and lower humidity (Perrone, 1979) is contributing to higher evaporation rates than in summer. In the Musa estuary, the relatively high evaporation combined with a limited exchange with the PG and shallow topography leads to the formation of high salinity, dense water mass and proposes a reverse estuary circulation pattern.

Tides in the PG are complex. The dominant tidal pattern changes from being primarily semidiurnal to diurnal (Mashayekh Poul et al., 2016; Pous et al., 2012; Reynolds, 1993). An inverse or negative estuary is a semi-enclosed sea or embayment within which loss of fresh water is more than the gain by runoff and precipitation combined.

There are two types of inverse estuaries depending on how the freshwater leaves estuary. The first type, when evaporation excess over precipitation in an arid area like the Red Sea, the Gulf of Suez, the Mediterranean Sea, the Adriatic Sea, the PG and in the Southern hemisphere, the South Australia gulfs and Shark Bay. In the second type, fresh water removes through freezing and the occurrence of sea ice. In both cases, since the net flux of mass is directed towards the head of the water body, contaminants will tend to congregate towards the head, rather than move into the ocean such as occurs in a classical estuary (Ansell et al., 1997).



Figure 46: satellite picture of the Musa estuary.

## 5.2 Model Description and Methods

The characteristics of tidal and density driven currents were investigated by using the vector ocean model shallow water, VOM-SW3d, and applied to the Musa estuary. The three dimensional model, like VOM-SW2d, is semi-implicit and nonlinear and was developed at the Institute of Oceanography at the University of Hamburg (Backhaus, 2008; Backhaus et al., 2008). The model domain spreads meridionally from 30.2 N to 30.5 N and zonally from 48.8 E to 49.3 E. It has a horizontal resolution of 150 meters with the Southern open boundary. The topography (Figure 47) is provided from interpolating measurement data on the satellite picture which has been used to produce a mask for the main channel, floodable and land area (Figure 48).



Figure 47: The topography of the Musa estuary (colorbar in meter). Redline shows the track line along the main channel.

VOM\_SW3D is applied in order to investigate the interaction between tidal wave and thermodynamic in an experimental slop to illustrate flow pattern of residual currents. Thereafter, it is applied to explore tide and density induced residual currents in Musa estuary with high resolution real topography. The model is forced at its open boundary by a sample wave with 1.5 m amplitude and period of 12 hours which is close to M2 tidal constituent.

VOM\_sw3d is updated to compute the evaporation rate and the heat fluxes at the surface (Figure 49). Heat transfer along the seabed changes seabed temperature and temperature of the last layer in the water column. Heat transfer along the surface changes salinity because of evaporation. Sea surface temperature changes via heat exchanges of the air-sea interface.



Figure 48: Different layers from satellite picture and measurement data, used for creating the topography of the Musa estuary.



Figure 49: Schematic diagram of heat fluxes on tidal flats. Arrows indicate the direction of heat flux.

In both studies, artificial and real Musa estuary domain, salinity and temperature are initialized with 36.5 and 28.5 degrees. At the open boundary, Newtonian boundary condition is used to prescribe salinity and temperature. The model computes the total amount of salt in the domain,  $\int_{1}^{lc3tot} hl \times S$ . Where hl is the cell height, S is salinity and lc3tot is the number of cells in vector-notation in the domain. Also, at the open boundary salinity anomaly is calculated to illustration the amount of saline water or salt which is produced by inverse estuary (Figure 50).



Figure 50: total salt in the domain, the output of salt from the open boundary and tidal elevation of the open boundary for 140 simulation days.

The structure of the residual circulation in the both studies is obtained by averaging the simulated horizontal momentum components, which includes the nonlinearity of interaction between tidal wave and topography, over hl (Babu et al., 2005; Quirós et al., 1992; Yuxiang, 1988). The same equation as section 3.3 is used here. The model is run for 140 days to reach the stationarity of salinity in the domain (Figure 51). This calculation is done for each component of horizontal velocities i.e., u and v. Thereafter, w is calculated from horizontal velocity fields.



Figure 51: Total salt in the domain, the output of salt from the open boundary and tidal elevation of the open boundary for the last 20 days of 140 days.

## 5.3 Results

## 5.3.1 Experimental domain

To investigate the mechanism of the inverse estuary and intricate interaction between tidal wave and bottom topography and density driven circulation, a numerical experiment is constructed with an artificial domain (2.5 km, 12 km). A channel created northward with a Dirichlet boundary condition at the southern boundary and a von Neumann boundary condition at the eastern and the western boundary. The northern boundary is closed with coastal slop. Applying the model to the test channel illustrated flow patterns of residual currents with and without thermodynamic effect.

Without thermodynamic effect, tidal residual currents create a vertical circulation with a landward current along the bottom and a seaward current at the surface (Figure 52). Vertical averaging over water columns indicates that velocity vectors tend to be normal to topography contours or flow patterns have a tendency to be proportional to the topographic slope which is in agreement with the previous 2D studies (Huthnance, 1973; Maas et al., 1987).



Figure 52: Tidally-averaged current velocity (colorbar in m/s) on the slope without the effect of thermodynamics. Vectors show the direction of the currents.

A significant residual tidal flow occurred landward near the bottom and seaward at the surface. As the effect of thermodynamics on the slope, the upstream bottom flow becomes weak and change to downstream. This is in agreement with a similar situation in the other estuaries (Blanton et al., 2003). Tidal flow causes turbulence throughout the water column and it increases mixing between the layers. Also, there is an inflow at the surface and outflow at the bottom near the open boundary (Figure 53).

Subtracting tidal residual current from velocity field shows the thermodynamic effect on residual currents on the slope (Figure 54). The currents are in opposite direction of the tidal residual current. Evaporation, caused by solar radiation, increases the salt content of the surface water and thus raises the density. As a result, dense water is created in the shallow coast of the domain. Saline water with a higher density sinks to the bottom and flows out from the seabed of the open boundary. It is replaced by an inflow of less salty water, caused by Newtonian boundary condition, at the surface.



Figure 53: Tidally-averaged current velocity (colorbar in m/s) on the slope with the effect of thermodynamics. Vectors show the direction of the currents.



Figure 54: Density-driven currents (colorbar in m/s) on the slop, the difference between Figure 52 and Figure 53. Vectors show the direction of the currents.

## 5.3.2 Musa estuary

After 120 days the model has reached the steady state in thermodynamics and in dynamics, as well. 3 tidal phases are shown each 4 hours later (Figures 55, 56 and 57). Upper left (UL) part of each figure shows the surface layer salinity and it varies from 36.5 at the open boundary to 60 in the shallow areas in the domain, which is the maximum limit for salinity in the model. In the tidal flat and shallow area because of the low water exchange salinity can reach to the maximum limit of the model. The lower left (LL) part of figures shows the zonal section (Z093) of salinity field close to the open boundary, which is marked with a white line in vertical grid-point, number 93, in UL. In this section, salinity varies between 36.5 and 40 during a tidal cycle in the main channel. The second channel in this section shows less variation in salinity, i.e. from 36.5 to 38.5. Going more inside to estuary, upper right part of the figures shows the meridional section (M163) in the deepest part of the domain. This is also marked with a white line in UL in horizontal grid-point, number 163, in UL. Here salinity changes from 39.8 to 41.4. The second meridional section (M316) is located in the center of the estuary, next to the port of Imam Khomeini. In this section, salinity varies between 41.5 and 44 during a tidal cycle. As the effect of evaporation and water exchange, salinity increases from the open boundary to the last section.



Figure 55: Model results for salinity (colorbar) after 120 days and 1 hour, UL: Surface layer. UR: Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL.



Figure 56: Model results for salinity (colorbar) after 120 days and 5 hours, UL: Surface layer. UR: Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL.



Figure 57: Model results for salinity (colorbar) after 120 days and 9 hours, UL: Surface layer. UR: Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL.

In all sections, the salinity contours are consistent with the contours of the normal component of current velocity.



Figure 58: Model results after 120 days and 12 hours for section Z093 in Musa estuary. Left: salinity (colorbar). Right: V-component of current velocity (colorbar in m/s). The section is marked in Figure 55.



Figure 59: Model results after 120 days and 18 hours for section Z093 in Musa estuary. Left: salinity (colorbar). Right: V-component of current velocity (colorbar in m/s). The section is marked in Figure 55.


Figure 60: Model results after 120 days and 12 hours for section M163 in Musa estuary. Left: salinity (colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure 55.



Figure 61: Model results after 120 days and 12 hours for section M163 in Musa estuary. Left: salinity (colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure 55.



Figure 62: Model results after 120 days and 12 hours for section M316 in Musa estuary. Left: salinity (colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure 55.



Figure 63: Model results after 120 days and 12 hours for section M316 in Musa estuary. Left: salinity (colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure 55.

Each section shows two tidal phases with 6 hours difference (Figures 58 to 63). In section Z093 current velocity varies between -2.0 to 2.3 m/s in two directions during one tidal cycle in the main channel. In section M163 maximum velocities are -1.9 and 2.3 m/s and in section M316 they velocity changes from -1.8 to 1.4 m/s.

An average of the simulated flow over one tidal cycle yields the residual circulation in the Musa estuary. Same as in the artificial domain the tidal flow effects the mixing between the layers. As a result, saline water transfers from the lower layers to the upper layers and some low salinity water from the surface towards the bottom. Generally, tidally-averaged salinity results in a horizontal salinity gradient with the salinity increasing towards the head of the Musa estuary. The averages for salinity and two horizontal components of currents along the track of the main channel are shown here (Figures 64, 65 and 66). Each part of tidally-averaged current velocity normal to the direction of the track (Figure 66) can be matched with a branch position in the topography.







Figure 65: Tidally-averaged current velocity (colorbar in m/s), in the direction of the track in the Musa estuary.



Figure 66: Tidally-averaged current velocity (colorbar in m/s), normal to the direction of the track in the Musa estuary.

This kind of situation can give rise to the formation of salt wedges, mainly during neap tide. In this situation, the tidal currents become weak and the tidal turbulence may not be able to break up the stratification, as, for example, in the Gulf St Vincent in South Australia (Ansell et al., 1997). As an effect of the topography, the circulation pattern is more complicated in the Musa estuary compared to the experimental domain.

Zonal and meridional sections are extracted to illustrate that salinity contours are consistent with the current velocity contours (Figures 67 and 68). High saline water outflow and low saline water inflow along with the stabilized salinity (Figure 51) in the whole region show that Musa estuary is a salt producer coastal system.



Figure 67: The model results in the meridional (M324) section in the Musa estuary for, Left: Tidally-averaged current velocity (colorbar in m/s), normal to the section, positive means inflow. Right: Tidally-averaged salinity (colorbar).



Figure 68: The model results in the zonal (Z036) section in the Musa estuary for, Left: Tidally-averaged current velocity (colorbar in m/s), normal to the section, positive means inflow. Right: Tidally-averaged salinity (colorbar).

### Chapter 6

### 6 Summary and Conclusions

The results of this study were achieved by improving the hydrodynamic numerical Vector-Ocean-Model (VOM) developed at the Institute für Meereskunde (IfM). A twodimensional shallow-water model has implemented for the PG. The model was forced by 13 tidal components at its open boundary to the Oman Sea. It reproduced well the tidal currents and elevations over the PG. The amphidromic points and the type of tidal variation (diurnal, semidiurnal, mixed) were also realistically reproduced. The model results were evaluated using data from 25 tidal gauges.

Strong tidal currents simulated by the model occurred in different parts of the PG for different types of constituents, in the second chapter. Maximum current speeds were found in the shallow regions of the PG. The results revealed that tides can provide a great amount of clean, kinetic energy in the PG on the Iranian side at the entrance of Musa estuary and Qeshm canal. However, prior to harnessing this power, some more geological and physical oceanographic studies are needed in this region. Also, it was found that tidal currents have an important effect on the hydrology of the whole PG. High amplitudes and extreme currents were found in Qeshm canal and also the effect of the topography of the canal on the propagation of tidal waves was described. Moreover, because of the flooding and drying ability of the model, the model better simulated the flooding of wide areas of the northern portion of the PG by tidal waves.

In chapter 3, the existence and the cause of a remarkable tidal residual eddy field are presented in the PG by resolving the impacts of geological structures i.e. salt domes beneath

the seabed, on the dynamics of the water column. It is very likely the richest barotropic eddy field ever observed in a marginal sea. The spatial structure of simulated residual currents was strongly influenced by nonlinear interactions of the tidal flow with the relief of the seabed. The latter resembling a shark-skin. That is, sub-seabed salt domes leave their signature in the tidal residual flow. In the high-pass filtered digital topography, more than 200 obstacles were observed which may have been caused by underlying salt domes. Only 60 salt domes have been charted so far by field work in oil exploration (Zaigham et al., 2013). Thus, the high-pass topography may provide further guidance for a future offshore exploration of mineral oil. Residual currents depicted by Lagrangian trajectories indicated the presence of strong coastal currents in the northern PG. There residuals of the M2 tide may exceed 0.15 m/s while tidal currents in that area were around 1.5 m/s. Spatial scales of the barotropic tidal residual eddies are in the order of 10 Km. The internal Rossby Radius of Deformation, a measure of the scales of baroclinic eddies in the PG, was of the same order. This agreement in scales suggests that barotropic and baroclinic eddies interact. This awaits future investigation.

In chapter 4, the model predicted resonance for both diurnal and semidiurnal constituents. Results reveal a system of amphidromic points of Kelvin-Taylor type with two points for semidiurnal constituents and a single point for diurnal constituents which agrees well with previous studies (Bosch van Drakestein, 2014; Hyder et al., 2013; Mashayekh Poul et al., 2016; Pous et al., 2013; Ranaee et al., 2012; Reynolds, 1993). The model results unveiled the following main features of tidal resonance in the PG:

- A. Diurnal tides were resonant in the northern PG and in the region off the Arabian coast.
- B. Semidiurnal tides were amplified in the northern Gulf and in the Strait of Hormuz.
- C. A simulated sea level rise increased AF in the region off the Arabian coast for semidiurnal and in the Qeshm Canal for both tides.
- D. The amphidromic points were displaced in position in the PG when different periods of forcing were used.
- E. The results revealed that tides can provide a great amount of potential energy in the Iranian side of the PG, at the Musa estuary and Qeshm canal.
- F. Semidiurnal tides provide more energy (10 times) compare to diurnal tides in the PG.

Finally, in chapter 5, the mechanism of tidal barotropic residual circulation in the Musa estuary was described by applying an updated version of VOM-SW3D with an additional

thermodynamic module into the Musa estuary. The main objective was to understand the effect of evaporation on density-driven circulation and its interactions with tidal currents. As a result of evaporation in this arid region, salinity increased in the surface layer and in shallow tidal flats. Dense near-bottom water flowed toward the PG and was replaced by an inflow of relatively fresh water at the surface. But, residual tidal currents flowed in the opposite direction. Variation in meteorological parameters and tidal amplitude controls the general circulation. The results revealed high salinity outflow and low salinity inflow along with the stabilized salinity in the whole region. A horizontal gradient in tidally-averaged salinity was found with the salinity increasing towards the head of the Musa estuary. The results suggest that the Musa estuary is a salt producing, coastal system.

## Acknowledgement

Thanks God, the almighty, for giving me strength, tolerance, patience and good luck that helped me to complete this work.

I would like to thank my supervisor, Professor Jan Backhaus. His interest in the field of numerical modeling, innovative ideas, valuable suggestions and sense of determination helped me during my PhD.

I am extremely grateful to Udo Huebner for all his help. Throughout my entire time at Hamburg, Jan and Udo have provided me with a great deal of support. I am very grateful to both of them.

I would like to thank my thesis committee members for all of their guidance through this process, especially, Dr. Thomas Pohlmann and Dr. Ali Dehghani.

I was lucky to have a great group of friends. In particular, thanks Dr. Moritz Mathis; his discussions and feedbacks have been invaluable.

The ministry of science, research and technology of Iran funded this research.

# Declaration

I hereby declare, on oath, that I have written the present dissertation by my own and have not used other than the acknowledged resources and aids.

Hamburg, 30.03.2016

Hossein Mashayekh Poul

## Bibliography

- Al-Subhi, A., 2010. Tide and Sea Level Characteristics at Juaymah, West Coast of the Arabian Gulf. J. King Abdulaziz Univ. Sci. 21, 133–149.
- Alvarez Fanjul, E., Gómez, B.P., Sánchez-Arévalo, I.R., 1997. A description of the tides in the Eastern North Atlantic. Prog. Oceanogr. 40, 217–244.
- Andersen, O.B., Egbert, G.D., Erofeeva, S.Y., Ray, R.D., 2006. Mapping nonlinear shallowwater tides: a look at the past and future. Ocean Dyn. 56, 416–429.
- Ansell, A., Gibson, R., Barnes, M., 1997. Oceanography and marine biology. An annual review. J. Mar. Biol. Assoc. United Kingdom 35, 653. doi:10.1017/S0025315400041795
- Arakawa, A., 1972. Design of the UCLA general circulation model. Numerical Simulation of Weather and Climate.
- Arakawa, A., Lamb, V.R., 1977. Computational Design of the Basic Dynamical Processes of the UCLA General Circulation Models of the Atmosphere, Methods in Computational Physics: Advances in Research and Applications, Methods in Computational Physics: Advances in Research and Applications. Elsevier.
- Arakawa, A., Schubert, W.H., 1974. Interaction of a Cumulus Cloud Ensemble with the Large-Scale Environment, Part I. J. Atmos. Sci. 31, 674–701.
- Arbic, B.K., St-Laurent, P., Sutherland, G., Garrett, C., 2007. On the resonance and influence of the tides in Ungava Bay and Hudson Strait. Geophys. Res. Lett. 34, L17606. doi:10.1029/2007GL030845
- Babu, M.T., Vethamony, P., Desa, E., 2005. Modelling tide-driven currents and residual eddies in the Gulf of Kachchh and their seasonal variability. Ecol. Modell. 184, 299–312.
- Backhaus, J., 1976. Zur Hydrodynamik im Flachwassergebiet. Ein numerisches Modell. Dtsch. Hydrogr. Zeitschrift 29, 222–238. doi:10.1007/BF02226256
- Backhaus, J.O., 2015. Latent resonance in tidal rivers, with applications to River Elbe. J. Mar. Syst. 151, 71–78.
- Backhaus, J.O., 2008. Improved representation of topographic effects by a vertical adaptive grid in vector-ocean-model (VOM). Part I: Generation of adaptive grids. Ocean Model. 22, 114–127.
- Backhaus, J.O., 1996. Climate-sensitivity of European marginal seas, derived from the interpretation of modelling studies. J. Mar. Syst. 7, 361–382.
- Backhaus, J.O., 1985. A three-dimensional model for the simulation of shelf sea dynamics. Dtsch. Hydrogr. Zeitschrift 38, 165–187.
- Backhaus, J.O., 1983. A semi-implicit scheme for the shallow water equations for application to shelf sea modelling. Cont. Shelf Res. 2, 243–254.

- Backhaus, J.O., Harms, I., Hübner, U., 2008. Improved representation of topographic effects by a vertical adaptive grid in Vector-Ocean-Model (VOM). Part II: Simulations in unstructured adaptive grids. Ocean Model. 22, 128–145.
- Badri, M.A., Wilders, P., 2012. Flow estimation for the Persian Gulf using a kelvin wave expansion. Indian J. Geo-Marine Sci. 41, 249–258.
- Bahaj, A.S., Myers, L., 2004. Analytical estimates of the energy yield potential from the Alderney Race (Channel Islands) using marine current energy converters. Renew. Energy 29, 1931–1945.
- Bakker, W.T., de Vriend, H.J., 1995. Resonance and morphological stability of tidal basins. Mar. Geol. 126, 5–18.
- Blain, C.A., 1998. Barotropic Tidal and Residual Circulation in the Arabian Gulf. Proc. 6th Int. Conf. Estuar. Coast. Model. 166–180.
- Blain, C.A., n.d. Modeling Three-Dimensional, Thermohaline-Driven Circulation in the Arabian Gulf, in: Estuarine and Coastal Modeling (1999). ASCE, pp. 74–93.
- Blanton, J.O., Seim, H., Alexander, C., Amft, J., Kineke, G., 2003. Transport of salt and suspended sediments in a curving channel of a coastal plain estuary: Satilla River, GA. Estuar. Coast. Shelf Sci. 57, 993–1006. doi:10.1016/S0272-7714(03)00005-2
- Bosch van Drakestein, F.G., 2014. Modeling of tides and spreading of saline water in the Arabian Gulf and in the coastal area of Abu Dhabi with a flexible mesh model.
- Brewer, P.G., Dyrssen, D., 1985. Chemical oceanography of the Persian Gulf. Prog. Oceanogr. 14, 41–55.
- Carbajal, N., Backhaus, J.O., 1998. Simulation of tides, residual flow and energy budget in the Gulf of California. Oceanol. Acta 21, 429–446.
- Chao, S.-Y., Kao, T.W., Al-Hajri, K.R., 1992. A Numerical Investigation of Circulation in the Arabian Gulf. J. Geophys. Res. 97, 11219–11236. doi:10.1029/92jc00841
- Chen, W., Liu, W., Hsu, M., 2013. Modeling Evaluation of Tidal Stream Energy and the Impacts of Energy Extraction on Hydrodynamics in the Taiwan Strait 2191–2203. doi:10.3390/en6042191
- Chu, P.C., Williams, C.L., Clem, T., Haeger, S.D., Ward, M., 2008. Environmental impact on chemical/oil spill in the Persian Gulf. Environ. Probl. Coast. Reg. VII I, 149–159. doi:10.2495/CENV080141
- Davies, A.M., Jones, J.E., 1996. Sensitivity of Tidal Bed Stress Distributions, Near-Bed Currents, Overtides, and Tidal Residuals to Frictional Effects in the Eastern Irish Sea. J. Phys. Oceanogr. 26, 2553–2575.
- Defant, A., 1961. Physical oceanography. Pergamon Press, New York.
- Dworak, J.A., Gómez-Valdés, J., 2003. Tide-induced residual current in a coastal lagoon of the Gulf of California. Estuar. Coast. Shelf Sci. 57, 99–109.

- Edgell, H., 1991. Proterozoic salt basins of the Persian Gulf area and their role in hydrocarbon generation. Precambrian Res. 54, 1–14.
- Egbert, G.D., Erofeeva, S.Y., 2002. Efficient Inverse Modeling of Barotropic Ocean Tides. J. Atmos. Ocean. Technol. 19, 183–204.
- El-Sabh, M.I., Murty, T.S., 1989. Storm surges in the Arabian Gulf. Nat. Hazards 1, 371–385.
- Emery, K.O., 1956. Sediments and Water of Persian Gulf. Am. Assoc. Pet. Geol. Bull. 40, 2354–2383.
- Ezam, M., Bidokhti, a. a., Javid, a. H., 2010. Numerical simulations of spreading of the Persian Gulf outflow into the Oman Sea. Ocean Sci. 6, 887–900.
- Ganj, M., 2013. Simulation of Tidal Currents in the Persian Gulf. Int. J. Emerg. Trends Eng. Dev. 5, 31–38.
- Garrett, C., 1972. Tidal Resonance in the Bay of Fundy and Gulf of Maine. Nature 238, 441–443. doi:10.1038/238441a0
- Godin, G., 1993. On tidal resonance. Cont. Shelf Res. 13, 89–107.
- Goharnejad, H., Shamsai, A., Hosseini, S.A., 2013. Vulnerability assessment of southern coastal areas of Iran to sea level rise: evaluation of climate change impact. Oceanologia 55, 611–637.
- Gorji-Bandpy, M., Azimi, M., Jouya, M., 2013. Tidal Energy and Main Resources In the Persian Gulf. Distrib. Gener. Altern. Energy J. 28, 61–77.
- Hainbucher, D., Backhaus, J.O., 1999. Circulation of the eastern North Atlantic and northwest European continental shelf - a hydrodynamic modelling study. Fish. Oceanogr. 8, 1–12.
- Harms, I.H., Heath, M.R., Bryant, A.D., Backhaus, J.O., Hainbucher, D.A., 2000. Modelling the Northeast Atlantic circulation: implications for the spring invasion of shelf regions by Calanus finmarchicus. ICES J. Mar. Sci. 57, 1694–1707.
- Hill, D.F., Griffiths, S.D., Peltier, W.R., Horton, B.P., Törnqvist, T.E., 2011. High-resolution numerical modeling of tides in the western Atlantic, Gulf of Mexico, and Caribbean Sea during the Holocene. J. Geophys. Res. Ocean. 116, 1–16.
- Hosseinibalam, F., Hassanzadeh, S., Rezaei-Latifi, a., 2011. Three-dimensional numerical modeling of thermohaline and wind-driven circulations in the Persian Gulf. Appl. Math. Model. 35, 5884–5902. doi:10.1016/j.apm.2011.05.040
- Huang, D., Su, J., Backhaus, J.O., 1999. Modelling the seasonal thermal stratification and baroclinic circulation in the Bohai Sea. Cont. Shelf Res. 19, 1485–1505.
- Huthnance, J.M., 1973. Tidal current asymmetries over the Norfolk Sandbanks. Estuar. Coast. Mar. Sci. 1, 89–99.
- Hyder, P., While, J., Arnold, A., O Dea, E., Furner, R., Siddorn, J., Martin, M., Sykes, P.,

2013. Evaluating a new NEMO-based Persian/Arabian Gulf tidal operational model. J. Oper. Oceanogr. 6, 3–16.

- Janssen, F., Schrum, C., Hübner, U., Backhaus, J.O., 2001. Uncertainty analysis of a decadal simulation with a regional ocean model for the North Sea and Baltic Sea. Clim. Res. 18, 55–62.
- John, V.C., 1992. Harmonic tidal current constituents of the western Arabian Gulf from moored current measurements. Coast. Eng. 17, 145–151.
- Johns, W.E., Yao, F., Olson, D.B., Josey, S.A., Grist, J.P., Smeed, D.A., 2003. Observations of seasonal exchange through the Straits of Hormuz and the inferred heat and freshwater budgets of the Persian Gulf. J. Geophys. Res.
- Kent, P.E., 1979. THE EMERGENT HORMUZ SALT PLUGS OF SOUTHERN IRAN. J. Pet. Geol. 2, 117–144. doi:10.1111/j.1747-5457.1979.tb00698.x
- Komen, G.J., Riepma, H.W., Bilt, D., 1981. The generation of residual vorticity by the combined action of wind and bottom topography in a shallow sea. Oceanol. acta 4, 267–278.
- Lavín, M.F., Marinone, S.G., 2003. An overview of the physical oceanography of the Gulf of California. Nonlinear Process. Geophys. Fluid Dyn.
- Le Provost, C., Fornerino, M., 1985. Tidal Spectroscopy of the English Channel with a Numerical Model. J. Phys. Oceanogr. 15, 1009–1031.
- Le Souëf, K.E., Allen, S.E., 2014. Physical modeling of tidal resonance in a submarine canyon. J. Geophys. Res. Ocean. 119, 1324–1343.
- Lewis, J.K., Vayda, G.A., Hsu, Y.L., 1968. a Coupled Regional Tide Model. US Pat. 3,371,052.
- Liang, D., Xia, J., Falconer, R. a., Zhang, J., 2014. Study on Tidal Resonance in Severn Estuary and Bristol Channel. Coast. Eng. J. 56, 1450002.
- Lokier, S.W., Bateman, M.D., Larkin, N.R., Rye, P., Stewart, J.R., 2015. Late Quaternary sea-level changes of the Persian Gulf. Quat. Res. 84, 69–81.
- Maas, L.R.M., Zimmerman, J.T.F., Temme, N.M., 1987. On the Exact Shape of the Horizntal Profile of a Topographically Rectified Tidal Flow. Geophys. Astrophys. Fluid Dyn. 38, 105–129.
- Marinone, S.G., 1997. Tidal residual currents in the Gulf of California: Is the M2 tidal constituent sufficient to induce them? J. Geophys. Res. 102, 8611–8623.
- Mashayekh Poul, H., Backhaus, J., Huebner, U., 2016. A description of the tides and effect of Qeshm canal on that in the Persian Gulf using two-dimensional numerical model. Arab. J. Geosci. 9, 148. doi:10.1007/s12517-015-2259-8
- Mashayekh Poul, H., Backhaus, J.O., Huebner, U., 2014. Estimate the area with most efficiency for producing energy from tide in the Persian Gulf, in: The 11th International

Conference on Coasts, Ports and Marine Structures. Tehran, Iran.

- McMillan, J., Lickley, M., 2008. The Potential of Tidal Power from the Bay of Fundy. SIAM Undergrad. Res. Online 1, 20–37.
- Moeini, M.H., Etemad-Shahidi, A., Chegini, V., 2010. Wave modeling and extreme value analysis off the northern coast of the Persian Gulf. Appl. Ocean Res. 32, 209–218.
- Najafi, H.S., 1997. Modelling tides in the Persian Gulf using dynamic nesting. University of Adelaide.
- Nicholls-Lee, R.F., 2011. Adaptive Composite Blades for Horizontal Axis Tidal Turbines. University of Southampton.
- Pawlowicz, R., Beardsley, B., Lentz, S., 2002. Classical tidal harmonic analysis including error estimates in MATLAB using T\_TIDE. Comput. Geosci. 28, 929–937.
- Perotti, C.R., Carruba, S., Rinaldi, M., Bertozzi, G., Feltre, L., Rahimi, M., 2011. New Frontiers in Tectonic Research At the midst of Plate Convergence. InTech.
- Perrone, T.J., 1979. Winter Shamal in the Persian Gulf.
- Pous, S., Carton, X., Lazure, P., 2013. A Process Study of the Wind-Induced Circulation in the Persian Gulf. Open J. Mar. Sci. 03, 1–11. doi:10.4236/ojms.2013.31001
- Pous, S., Carton, X., Lazure, P., 2012. A Process Study of the Tidal Circulation in the Persian Gulf. Open J. Mar. Sci. 02, 131–140. doi:10.4236/ojms.2012.24016
- Pous, S., Lazure, P., Carton, X., 2015. A model of the general circulation in the Persian Gulf and in the Strait of Hormuz: Intraseasonal to interannual variability. Cont. Shelf Res. 94, 55–70. doi:10.1016/j.csr.2014.12.008
- Pous, S.P., Carton, X., Lazure, P., 2004a. Hydrology and circulation in the Strait of Hormuz and the Gulf of Oman-Results from the GOGP99 Experiment: 2. Gulf of Oman. J. Geophys. Res. C Ocean. 109, 1–15.
- Pous, S.P., Carton, X., Lazure, P., 2004b. Hydrology and circulation in the Strait of Hormuz and the Gulf of Oman — Results from the GOGP99 Experiment : 1 . Strait of Hormuz Hydrology and circulation in the Strait of Hormuz and the Gulf of Oman; results from the GOGP99 Experiment . Part I . Strai. J. Geophys. Res. 109.
- Proudman, J., 1953. Dynamical Oceanography. Methuen & Co.
- Purser, B.H., 1973. Sedimentation around bathymetric highs in the southern Persian Gulf. Persian Gulf 157–177.
- Quaresma, L.S., Pichon, A., 2013. Modelling the barotropic tide along the West-Iberian margin. J. Mar. Syst. 109-110, S3–S25.
- Quirós, G., Badan-Dangon, A., Ripa, P., 1992. M2 currents and residual flow in the Gulf of California. Netherlands J. Sea Res. 28, 251–259.
- Ranaee, E., Mosaddad, S.M., Akbari, M., 2012. Seasonal Influences of Boundary Conditions

in Coastal Water Quality Variations (Case Study: Northern Zone of Persian Gulf) Faculty of Physical Oceanography, Young Researchers Club, World Appl. Sci. J. 19, 894–903.

- Ranaee, E., Mosaddad, S.M., Akbari, M., 2011. Seasonal Influences of Boundary Conditions in Coastal Water Quality Variations. World Appl. Sci. J. 13.
- Reynolds, M., 1993. Physical oceanography of the Gulf, Strait of Hormuz, and the Gulf of Oman—Results from the Mt Mitchell expedition. Mar. Pollut. Bull. 27, 35–59.
- Robinson, I.S., 1981. Tidal vorticity and residual circulation. Deep Sea Res. Part A. Oceanogr. Res. Pap. 28, 195–212.
- Roos, P.C., Schuttelaars, H.M., 2010. Influence of topography on tide propagation and amplification in semi-enclosed basins. Ocean Dyn. 61, 21–38.
- Sabbagh Yazdi, S.R., Sadeghi Gooya, A., 2010. Modeling Khowr-e Musa Multi-Branch Estuary Currents due to the Persian Gulf Tides Using NASIR Depth Average Flow Solver. J. Persian Gulf 1, 45–50.
- Sabbagh-Yazdi, S.-R., Zounemat-Kermani, M., Kermani, A., 2007. Solution of depthaveraged tidal currents in Persian Gulf on unstructured overlapping finite volumes. Int. J. Numer. Methods Fluids 55, 81–101.
- Sarnthein, M., 1972. Sediments and history of the Postglacial transgression in the Persian Gulf and northwest Gulf of Oman. Mar. Geol. 12, 245–266.
- Schrum, C., Backhaus, J.O., 1999. Sensitivity of atmosphere-ocean heat exchange and heat content in the North Sea and the Baltic Sea. Tellus A 51, 526–549.
- Seni, S.J., Jackson, M.P.A., 1984. SEDIMENTARY RECORD OF CRETACEOUS AND TERTIARY SALT MOVEMENT, EAST TEXAS BASIN; Times, Rates, and Volumes of Salt Flow and Their Implications for Nuclear Waste Isolation and Petroleum Exploration.
- Skiba, A.W., Zeng, L., Arbic, B.K., Müller, M., Godwin, W.J., 2013. On the Resonance and Shelf/Open-Ocean Coupling of the Global Diurnal Tides. J. Phys. Oceanogr. 43, 1301– 1324.
- Stronach, J.A., Backhaus, J.O., Murty, T.S., 1993. An update on the numerical simulation of oceanographic processes in the waters between Vancouver Island and the mainland: the GF8 model. Oceanogr. Mar. Biol. An Annu. Rev. 31, 1–86.
- Sutherland, G., Garrett, C., Foreman, M., 2005. Tidal Resonance in Juan de Fuca Strait and the Strait of Georgia. J. Phys. Oceanogr. 35, 1279–1286.
- Swift, S.A., Bower, A.S., 2003. Formation and circulation of dense water in the Persian/Arabian Gulf. J. Geophys. Res. 108, 3004.
- Thomas, R.J., Ellison, R. a., Goodenough, K.M., Roberts, N.M.W., Allen, P. a., 2015. Salt domes of the UAE and Oman: Probing eastern Arabia. Precambrian Res. 256, 1–16.

- Thoppil, P.G., Hogan, P.J., 2010a. Persian Gulf response to a wintertime shamal wind event. Deep Sea Res. Part I 57, 946–955.
- Thoppil, P.G., Hogan, P.J., 2010b. A Modeling Study of Circulation and Eddies in the Persian Gulf. J. Phys. Oceanogr. 40, 2122–2134. doi:10.1175/2010JPO4227.1
- Westerink, J.J., Stolzenbach, K.D., Connor, J.J., 1989. General Spectral Computations of the Nonlinear Shallow Water Tidal Interactions within the Bight of Abaco. J. Phys. Oceanogr. 19, 1348–1371.
- Yao, F., 2008. Water Mass Formation and Circulation in the Persian Gulf, and Water Exchange with the Indian Ocean The Hydrogaphy and Circula-. Univ. Miami. university of Miami.
- Yuxiang, T., 1988. Numerical modelling of the tide-induced residual current in the East China Sea. Prog. Oceanogr. 21, 417–429.
- Zaigham, N.A., Aburizaiza, O.S., Nayyer, Z.A., Mahar, G.A., Siddique, A., 2013. Salt-Tectonics Plays Major Role in Contributing High Seawater Salinity in Arabian / persian Gulf: A Constant Constrain on Seawater Desalination. Int. J. Water Resour. Arid Environ. 2, 187–194.
- Zimmerman, J.T.F., 1978. Hydrodynamics of Estuaries and Fjords, Proceedings of the 9th International Liege Colloquium on Ocean Hydrodynamics, Elsevier Oceanography Series, Elsevier Oceanography Series. Elsevier.

## Appendix

If not cited otherwise in the text, the information is summarized from (Backhaus, 2008, 1985, 1983; Backhaus et al., 2008) and Script of "Introduction to Modelling of Ocean Physics" from Prof. Dr. Jan O. Backhaus in University of Hamburg, Germany.

### **1** Theoretical Aspects of **2D** primitive equation models

### 1.1 Influence of the Spatial Discretization on Wave Propagation

Any discretization of the space domain when applied to an approximation of wave phenomena will inevitably introduce artificial i.e. numerical wave dispersion. This also applies to waves, void of dispersion as shown by an example of one-dimensional gravity waves. The following is an extract of an analysis published by Mesinger and Arakawa (1976).

One-dimensional non-rotational Gravity Waves; Artificial Dispersion

 $\mathbf{U}_{\mathbf{t}} = -\mathbf{g}\mathbf{h}_{\mathbf{x}}$  (equation of motion for velocity U)

 $\mathbf{h}_{t} = -\mathbf{H}\mathbf{U}_{x}$  (linearized equation of continuity for surface elevation h and depth H)

Wave- (Fourier-) approximations for velocity U and surface elevation h:

 $U = U_0 e^{i(kx-\omega t)}; \ h = h_0 e^{i(kx-\omega t)}$ 

Which in that k is wave-number (k= $2\pi/L$ ),  $\omega$  frequency, x and t space and time, U<sub>0</sub> and h<sub>0</sub> are amplitudes.

By inserting the wave-approximations into the differential equations, analytical solutions for U and h are obtained:

 $\omega U_0 = \mathbf{g} \mathbf{k} \mathbf{h}_0$  (equation of motion);  $\omega \mathbf{h}_0 = \mathbf{H} \mathbf{k} U_0$  (equation of continuity)

Inserting  $\mathbf{h}_0 = \mathbf{H}\mathbf{k}\mathbf{U}_0/\boldsymbol{\omega}$  from the equation of continuity into the solution of the equation of motion we arrive to  $\boldsymbol{\omega}\mathbf{U}_0 = \mathbf{g}\mathbf{k}(\mathbf{H}\mathbf{k}\mathbf{U}_0/\boldsymbol{\omega})$ , from which we readily obtain the dispersion relation for gravity waves:

$$(\omega/\mathbf{k})^2 = \mathbf{c}^2 = \mathbf{g}\mathbf{H}$$

The dispersion relation, also called 'frequency-wave-number relation' for gravity waves indicates that these waves are void of dispersion because the phase speed is not depending on wavelength (or wave-number) but only on water depth H.

Assume the above gravity wave equations are approximated by central differences in both space and time. Then wave-solutions when inserted into the difference approximations for U and h yield:

### $\omega^2 = gH(\sin(kd)/d)^2.$

In dividing this by k<sup>2</sup> we obtain the dispersion relation of the difference approximation:

### $(\omega/k)^2 = c^{*2} = gH(sin(kd)/kd)^2$

Where c\* is the 'numerical' phase velocity. Comparing true velocity and 'numerical' phase velocity we note that the latter contains the additional term:  $(\sin(kd)/kd)^2$  which indicates artificial i.e. 'numerical' dispersion.That is because the phase velocity c\* depends on wave number k. Other difference approximations applied to gravity waves would yield a similar result in that the phase velocity is modified by a term containing increment d and wave number k. Note that for  $\sin(kd) \sim kd$  i.e. for small increments d and/or small wavenumbers k (i.e. large wave-lengths) c\* approaches the true velocity c. However, for kd =  $\pi$  i.e. for L=2d the phase velocity c\* would always be zero.

#### **1.2** Spatial Discretisation for the 'Primitive' Equations

The Japanese meteorologist Arakawa was the first who systematically investigated the properties of various grids used to approximate the 'primitive equations' when applied to geostrophic adjustment (Arakawa and Schubert, 1974; Arakawa, 1972). Meteorologists call the vertically integrated shallow water (storm-surge) equations 'primitive equations'. Initially Arakawa carried out investigations of various grids for meteorological models in the 70ies of the last century, but they also apply for ocean models. Arakawa's original notation the primitive shallow water equations with a linearised equation of continuity, where (u,v) are flow components, h is surface elevation, and H water depth:

 $\partial u/\partial t = -g \partial h/\partial x + f v$  $\partial v/\partial t = -g \partial h/\partial y - f u$   $\partial h/\partial t = -H(\partial u/\partial x + \partial v/\partial y)$ 

### 1.3 Numerical Wave Dispersion in Arakawa C-Grid

Gravity-inertia waves, similar as pure gravity waves are non-dispersive. That is because their phase velocity  $\mathbf{c} = \sqrt{\mathbf{gH}}$  does not depend on wavelength or wave-number k, respectively. The group velocity of gravity-inertia waves  $V_g = \partial \omega / \partial \mathbf{k}$  is constant since the frequency increases monotonically with the wave-number k, which we see from the dispersion relation of gravity-inertia waves:

 $(\omega/f)^2 = 1 + (\lambda k)^2$ 

Here  $\lambda$  is the Rossby-Radius of Deformation  $\lambda = \sqrt{gH}/f$ ,  $\omega$  the frequency, f the Coriolis parameter,  $k = 2\pi/L$  the wavenumber with wavelength L.

Due to the constant slope of the 'true' 'analytic' dispersion relation (see graph below), the group velocity can never become zero, i.e. (wave-) disturbances always propagate and do not stagnate irrespective of wavenumber. Therefore, in a rotational adjustment under gravity (i.e. geostrophic adjustment) it is impossible that wave energy accumulates locally. Unfortunately, this is not the case with primitive equations approximated in discrete grids. In the following, wave dispersion is considered along one coordinate axis of two-dimensional Arakawa C-grid.

The approximation of the space domain by C-grid with spatial increments d causes 'Numerical Dispersion'. That is, a simulated gravity-inertia wave becomes increasingly dispersive with increasing k, i.e. for decreasing wavelengths. For the grids A to D the smallest resolvable wavelength is L = 2d, whereas for the E-grid this wavelength is:  $L = 2d/\sqrt{2}$ . Thus, in the graph below, for grids A to D a wavenumber ranges  $0 < kd < \pi$  applies, but for the E-grid the range is  $0 < kd < \sqrt{2} \pi$ . Note: the wave-number range in the graph has been normalised by  $\pi$ .

#### 1.4 Dispersion Relations of Arakawa C-Grids

Below the Arakawa grid C is given with its respective 'numerical' dispersion relation in which d is the spatial increment. In this relation, the frequency depends on two parameters: kd and  $\lambda/d$ . The below graph is drawn for  $\lambda/d=2$  i.e. for a Rossby-Radius of deformation that is covered by (just) two spatial increments d, i.e. a two delta L wave. This appears as ill-posed problem but it is to highlight effects of numerical dispersion. For  $\lambda=2d$  the 'true' dispersion relation of gravity-inertia waves given above modifies as follows:

 $(\omega/f)^2 = 1 + (\lambda k)^2 \rightarrow (\omega/f)^2 = 1 + (2kd)^2$ 

We compare this with the numerical dispersion relations of Arakawa C grid below.

$$(\omega/f)^2 = \cos^2(kd/2) + 4(\lambda/d)^2 \sin^2(kd/2)$$

For  $\lambda/d > 1/2$  the frequency increases monotonically until kd =  $\pi$  where it reaches its maximum implying zero group velocity for the smallest resolvable two-grid-interval wave. For  $\lambda/d < 1/2$  the frequency would decrease monotonically. For  $\lambda/d = 1/2$  the phase velocity is equal 1 for all k implying zero group velocity for all wave-numbers.



Figure 1: Comparison of frequency dispersion in various Arakawa grids

### 2 Rotational Primitive Equation Models; explicit, implicit

The Shallow Water Equations for a vertically integrated 2D ,Storm-Surge' Model in momentum-form read:

$$U_t + gH\zeta_x = X$$
  
 $V_t + gH\zeta_v = Y$ 

 $\zeta_t = -(U_x + V_y);$  (nonlinear Divergence, utilizing  $(Hu)_x, (Hv)_y)$ 

Momentum (Impuls) - Vector (U,V) = (Hu,Hv); H: actual water depth,  $\mathbf{H} = \mathbf{D} + \boldsymbol{\zeta}$ ; (u,v): Velocity Components; (X,Y): further (optional) terms, for instance horizontal diffusion, wind

stress and seabed friction, nonlinear momentum advection, or Coriolis terms. The Shallow Water Equations are a coupled system of three partial differential equations. Their explicit approximation requires fulfilling the, 'Courant-Friedrich-Lewy' (CFL) stability-criterion:

### $\Delta t \ \le \ \Delta L/\sqrt{2^{n-1}gH}$

The phase velocity in the denominator contains a power (n-1) which indicates the Dimension n of the problem (n=2 for 2D). g is earth acceleration. The CFL-criterion implies that the propagation of free surface waves may not be larger than the numerical Phase-Speed  $C_n = \Delta L/\Delta t$ . In other words, wave disturbances may propagate at maximum one spatial increment  $\Delta L$  per time step  $\Delta t$ . For deep Ocean regions, the CFL-criterion in particular may constitute a very stringent limitation of the time-step. An implicit scheme may then be quite helpful for it is independent of the CFL-criterion. However, below we at first introduce the explicit scheme for it is a component of the implicit one. For the approximation of the space domain of the 2D model (Figure 1) we utilise the Arakawa-C grid.

-								
NW	0		N	0		NE	0	
	+	×		+	×		+	×
i-1,j+1			i,j+	-1		i+1,	j+1	
W	0		С	0		Е	0	
	+	×		+	×		+	×
i-1,j			i,j			i+1,	j	
SW	0		S	0		SE	0	
	+	×		+	×		+	×
i-1,j-1			i,j-	1		i+1,	j-1	

Legend: Indexing (i,j) and compass-rose indexing of variables in the ,staggered' Arakawa C-Grid; locations of prognostic variables:  $o : v; x : u; +: \zeta$ . In the staggered C-grid the indexing comprises a grid point triple (+, x, o) under one and the same index (i,j) = C. The i-index counts in positive direction of the east x-axis whereas j counts positive along the y-axis. ( $x \rightarrow i; y \rightarrow j$ )

### 2.1 Explicit Scheme for the Storm Surge Model in the Arakawa C-grid

It is only possible to solve the coupled system of equation of continuity and motion explicitly if we separate the prognostic variables by half a time-step. Thus updating the equation of continuity needs a velocity divergence at time-level n. This yields a new surface elevation at time-level n+1/2, which in turn serves to update momentum to time-level n+1. In practise, the staggered indexing in time is of no relevance. It is simply the sequence of computations that allows solving the system by using the respective newest results of either  $\zeta$  or (U,V).

The Equations of motion (1.e, 2.e) and of continuity (3.e) ('e' for explicit) read:

$$U_{c}^{n+1} = U_{c}^{n} - gHU_{c}^{n} dt/dx (\zeta_{e} - \zeta_{c})^{n+1/2} + dtX^{n}$$
(1.e)  

$$V_{c}^{n+1} = V_{c}^{n} - gHV_{c}^{n} dt/dy (\zeta_{n} - \zeta_{c})^{n+1/2} + dtY^{n}$$
(2.e)  

$$\zeta_{c}^{n+1/2} = \zeta_{c}^{n+1/2} - dt((U_{c} - U_{w})^{n}/dx + (V_{c} - V_{s})^{n}/dy)$$
(3.e)

The actual water depths at time-level n, averaged on momentum-locations, are:

$$HU_c^n = (D_e + D_c + \zeta_e + \zeta_c)^{n/2}$$
$$HV_c^n = (D_n + D_c + \zeta_n + \zeta_c)^{n/2}$$

with the undisturbed water depth D (topography) defined at location of  $\zeta$  (+).

Applying the difference scheme (1.e, 2.e, 3.e) of the storm surge model in a domain with tidal or wind forcing, and within the limits of the CFL stability-criterion, it would yield a stable solution. With an arbitrary topography, to ensure that the normal flux boundary condition always applies at closed boundaries (coast) we only compute a momentum component if both neighbouring  $\zeta$ -points are 'wet'. That concerns  $\zeta_e$  and  $\zeta_c$  for the east component, and  $\zeta_n$  and  $\zeta_c$  for the north component. 'Wet' implies that  $H = D + \zeta > 0$ . Later we will 'fill' (X,Y) with life, i.e. implement further terms.

#### 2.2 The implicit Storm Surge Model

Again (as in the 1D implicit channel) we apply a Cranck-Nicholson approach to yield an implicit system:  $\mathbf{p}\boldsymbol{\phi}_x^{n+1} + (\mathbf{1} - \mathbf{p})\boldsymbol{\phi}_x^n$ , with the Cranck-Nicholson Pointer p. We obtain an explicit scheme for  $\mathbf{p} = 0$ . The best choice for p is  $\mathbf{p}=1/2$  (neutral regarding damping). In the implicit scheme we do not have time-levels  $\mathbf{n} + \mathbf{1/2}$ .

Cranck-Nicholson Approach applied to the free surface gradients in the equations of motion (see Compass-rose Indexing in C-Grid above) where terms defined at 'old' time-level n are comprised in the ,Interim-Solution'  $(\mathbf{U}^*, \mathbf{V}^*)$  which is the explicit component:

Implicit equations of motion:

$$\mathbf{U}_{c}^{n+1} = \mathbf{U}^{*} - \mathbf{g}\mathbf{p}\mathbf{H}\mathbf{U}_{c}^{n}\,\mathbf{d}t/\mathbf{d}x\,(\boldsymbol{\zeta}_{e} - \boldsymbol{\zeta}_{c})^{n+1} \tag{1.i}$$

$$\mathbf{V}_{c}^{n+1} = \mathbf{V}^{*} - \mathbf{g}\mathbf{p}\mathbf{H}\mathbf{V}_{c}^{n}\,\mathbf{d}t/\mathbf{d}y\,(\boldsymbol{\zeta}_{n} - \boldsymbol{\zeta}_{c})^{n+1} \tag{2.i}$$

Explicit Interim solution of momentum:

 $U^{*} = U_{c}^{n} - g(1-p)HU_{c}^{n} dt/dx (\zeta_{e} - \zeta_{c})^{n} + dtX^{n}$ (1.1)

 $V^* = V_c^n - g(1-p)HV_c^n dt/dy (\zeta_n - \zeta_c)^n + dtY^n (2.1)$ 

Cranck-Nicholson Approach applied to momentum divergences in the Equation of Continuity.

$$\zeta_{c}^{n+1} = \zeta_{c}^{n} - dt \begin{pmatrix} p((U_{c} - U_{w})^{n+1}/dx + (V_{c} - V_{s})^{n+1}/dy) \\ + (1 - p)((U_{c} - U_{w})^{n}/dx + (V_{c} - V_{s})^{n}/dy) \end{pmatrix}$$
 to be replaced  
(3.i)

Similar as for the 1D channel model (chapter 2) we replace divergences at time level n+1 in (3.i) by the equation of motion (1.i, 2.i). After this replacement, the equation of continuity mutates to a linear system of equations (4i) in which the only unknown is the free surface elevation  $\zeta^{n+1}$ :

$$\begin{split} \zeta_c^{n+1} &= \zeta_c^* + g(pdt/dx)^2 H U_c (\zeta_e - \zeta_c)^{n+1} - g(pdt/dx)^2 H U_w (\zeta_c - \zeta_w)^{n+1} + \\ g(pdt/dy)^2 H V_c (\zeta_n - \zeta_c)^{n+1} - g(pdt/dy)^2 H V_s (\zeta_c - \zeta_s)^{n+1} \end{split} \tag{4i}$$

In (4i) terms defined at the ,old' time-level n, which can be obtained explicitly, are grouped together in  $\boldsymbol{\zeta}^*$  (4.1).

The explicit , interim-solution' of the free surface (4.1):

$$\begin{aligned} \zeta_c^* &= \zeta_c^n - dtp((U_c - U_w)^*/dx + (V_c - V_s)^*/dy) - dt(1 - p)((U_c - U_w)^n/dx + (V_c - V_s)^n/dy) \end{aligned} \tag{4.1}$$

The interim-solution (4.1) combines a divergence of the interim momentum  $(\mathbf{U}^*, \mathbf{V}^*)$  i.e. (1.1, 2.1) and of 'old' momentum-components at time-level n. It forms the solution vector of the elliptic system (5i) for  $\boldsymbol{\zeta}^{n+1}$  below.

Introducing coefficients CX, CY and sorting for time-levels system (4i) obtains the pentadiagonal form (5i), i.e. five unknowns appear on the left hand side. Note coefficients are defined at the locations of momentum-components. Index C indicates location (i,j) of a component if CX or Cy are concerned, whereas it is the location of the pressure point when  $\boldsymbol{\zeta}$ is concerned. The same rule applies for other compass-rose indices.

The elliptic implicit system of equations for the free surface elevation (5i):

 $-CX_{c}\zeta_{e}^{n+1}-CX_{w}\zeta_{w}^{n+1}+CC\zeta_{c}^{n+1}-CY_{c}\zeta_{n}^{n+1}-CY_{s}\zeta_{s}^{n+1}=\zeta_{c}^{*}$  (5i) central coefficient:  $CC = 1+CX_{c}+CX_{w}+CY_{c}+CY_{s}$ 

$$CX_c = g(p dt/dx)^2 HU_c$$
;  $CY_c = g(p dt/dy)^2 HV_c$ 

Coefficients  $CX_w$  and  $CY_s$  in (5i) are defined at location (i-1,j) (for U-component) and at (i,j-1) (for V-component), respectively.

Solving system (5i) with Successive Over-Relaxation (SOR)

We cannot solve the penta-diagonal system (5i) with the Gauss-Algorithm because it can only handle a tri-diagonal matrix. The alternative to direct elimination is an iteration scheme (see script Numerik), and we choose SOR (Successive Over-Relaxation). The iterative solution of system (5i) for  $\zeta^{n+1}$  involves a number of SORiterations L that are to be carried out at each time step. Define the residual  $\delta_c^L$  (6) for each grid point from the 'past' SOR step L:

$$\delta_{\mathbf{c}}^{\mathbf{L}} = \mathbf{C}\mathbf{C}\boldsymbol{\zeta}_{\mathbf{c}}^{\mathbf{L}} - (\mathbf{C}\mathbf{X}_{\mathbf{c}}\boldsymbol{\zeta}_{\mathbf{e}}^{\mathbf{L}} + \mathbf{C}\mathbf{X}_{\mathbf{w}}\boldsymbol{\zeta}_{\mathbf{w}}^{\mathbf{L}} + \mathbf{C}\mathbf{Y}_{\mathbf{c}}\boldsymbol{\zeta}_{\mathbf{n}}^{\mathbf{L}} + \mathbf{C}\mathbf{Y}_{\mathbf{s}}\boldsymbol{\zeta}_{\mathbf{s}}^{\mathbf{L}}) - \boldsymbol{\zeta}_{\mathbf{c}}^{*}$$
(6)

We observe that residual  $\delta_c^L$  is the difference between the left hand side of (5i) and its solution vector. The residual would be zero if the solution of system (5i) would be exact, i.e. the smaller the residual the closer is the solution. In iterations, an exact solution is rarely achieved because of round-off errors of the computer. Instead a solution is sought which satisfies (5i) with a defined accuracy  $\varepsilon$ . The accuracy  $\varepsilon$  should be oriented at the word length of the respective machine. For a 32 bit CPU this is ~ 10-6. (see script Numerik: iterative schemes)

We apply the Successive Over-Relaxation (SOR) Iteration (7) to all cells in a domain. Thus, one sweep over the domain comprises an iteration step that delivers a new estimate of  $\zeta^{L+1}$ .

$$\zeta_{\rm c}^{\rm L+1} = \zeta_{\rm c}^{\rm L} - \omega \delta_{\rm c}^{\rm L} / \rm C C \tag{7}$$

Relaxation-Parameter  $\omega$  is valid for  $1 < \omega < 2$ . For  $\omega < 1$  ,Under-Relaxation' is obtained. Usually over-relaxation gives the fastest ,convergence', i.e. the least number of iteration steps. Over-relaxation implies multiplying residual  $\delta_c^L$  (7) with an  $\omega > 1$ . For each iteration step L+1 we need to compute a new residual  $\delta_c^L$  and to determine the global norm  $N_{sor}$ , i.e. the maximum of deviations between old and new solution over all grid points:

$$\mathbf{N}_{sor} = \max \left| \boldsymbol{\zeta}^{\mathsf{L}+1} - \boldsymbol{\zeta}^{\mathsf{L}} \right| \tag{8}$$

The iteration is stopped, i.e. considered as convergent, if  $N_{sor} < \epsilon$ . After SOR has converged we obtain the desired (approximate) solution i.e.  $\zeta^{n+1} = \zeta^{L+1}$ .

The iteration would converge for any initial values because (5i) has elliptic character. That is the solution only depends on boundary values, the solution vector, and coefficients. Usually an iteration for  $\zeta^{L=1}$  is initialised with the solution of the previous time-step n. The right choice of the Relaxation-Parameter  $\omega$  has a strong impact on convergence-speed, i.e. the number of iterations that are needed to satisfy the

norm  $N_{sor}$ ; apparently, the fewer iterations the better. In oceanographic applications with complex topography, we recommend to determine Parameter  $\omega$  empirically.

The introduction of Chessboard-SOR will further increase convergence speed (see script Numerik): divide the iteration matrix into 'white' and 'black' cells as in a chessboard. Solving SOR (7) first for all black cells yields that all of the white cells solved subsequently will use already updated data from the black ones. This simple 'kunstgriff' allows significantly improving convergence-speed.

In oceanographic applications with arbitrary topography the normal condition, i.e. the no-flux condition at closed boundaries has to be satisfied. This boundary condition enters system (5i) via coefficients CX, CY (see chapter 2). Momentum-components situated at a closed boundary must be zero because one of the two neighbouring cells is dry. The same applies for the coefficients since they are defined at the location of the respective component. Note that coefficients are time-dependent for they contain the free surface elevation in the actual water depth HU, HV and, optionally, the friction functions SX, SY (see below).

Obtaining the solution for  $(U, V)^{n+1}$ 

Having solved system (5i) with the help of SOR-iteration (7) the free surface elevation  $\zeta^{n+1}$  is known for all grid points in the domain. This allows solving  $(U, V)^{n+1}$  from (1.i) and (2.i) by applying the free surface gradients at time-level n+1 to interim solutions.

$U_c^{n+1} = U^* - gpHU_c^n dt/dx  (\zeta_e - \zeta_c)^{n+1}$	(1.i)
$V_c^{n+1} = V^* - g p H V_c^n  dt/dy  (\zeta_n - \zeta_c)^{n+1}$	(2.i)
Subtract surface gradients	

This finalises the operations needed to solve one time-step in the 2D model. Note that with the exception of factor (1-p) the computation of interim-vector  $(\mathbf{U}, \mathbf{V})^*$  from (1.1) and (2.1) is identical to the explicit approximation (1.e, 2.e). Thus, as for the 1D channel, the explicit scheme forms a central part of the implicit one.

Sequence of Operations for one time step

Prior to SOR-Iteration:

Compute interim-solution  $\mathbf{U}^*$ ,  $\mathbf{V}^*$  (2.1, 2.2) and coefficients CX,CY,CC

Compute interim-solution  $\boldsymbol{\zeta}^*$  (4.1) from flow divergence

SOR Iteration: sweep over all cells in domain:

Compute residual  $\delta_c^L$  (6) from coefficients and previous  $\zeta$ 

Apply SOR-Relation (7) Check Norm (8) If not convergent: perform next sweep Else: stop iteration; compute (**U**, **V**)<sup>**n**+1</sup> from (1i, 2i)

Modifications for semi-implicit seabed friction

An explicit treatment of seabed friction, for instance  $U^{n+1} = U^n + \dots - U^n r dt \, SX^n / H U^2$ 

would yield:  $U^{n+1} = U^n/(1 - rdt SX^n/HU^2)$ . This approximation is dangerous because the term in the bracket may become smaller than one. In that event friction would change the sign of the flow which is against the first law of thermodynamics.

A better approach is a semi-implicit approximation:  $U^{n+1} = U^n + \dots - U^{n+1} r dt SX^n / HU^2$  in which there is a mixture of time-levels. This yield:  $U^{n+1} = U^n / (1 + r dt SX^n / HU^2)$ .

Clearly, in this approximation a change of the sign of flow is impossible.

Introducing a semi-implicit seabed friction in the storm surge model implies the following changes in the equations of motion (1.i) and (2.i):

$$\begin{split} & U^{n+1} = U^* - gSxHU^n \, dt/dx \, p(\zeta_e - \zeta_c)^{n+1} \\ & (1.i) \\ & V^{n+1} = V^* - gSyHV^n \, dt/dy \, p(\zeta_n - \zeta_c)^{n+1} \\ & (2.i) \\ & \text{Then the ,Interim-Solution'} \, (U^*, V^*) \text{reads:} \\ & U^* = Sx(U^n + dtX^n - gHU^n \, dt/dx \, (1 - p)(\zeta_e - \zeta_c)^n) \\ & (1.1) \\ & V^* = Sy(V^n + dtY^n - gHV^n \, dt/dy \, (1 - p)(\zeta_n - \zeta_c)^n) \\ & (2.1) \\ & Sx = 1/(1 + rdt(U^2 + VatU^2)^{1/2}/HU^2); \\ & Sy = 1/(1 + rdt(V^2 + UatV^2)^{1/2}/HV^2) \end{split}$$

Since momentum-components are defined at different locations (see figure C-grid above) we need to introduce spatial averages to obtain information about momentum at a location. Thus, UatV and VatU are 4 point averages located at the respective component where needed. With friction-functions Sx, Sy the coefficients(**CX**, **CY**) of system (5i) now read:

$$CX_c = gSx_c(p dt/dx)^2 HU_c;$$
  $CY_c = gSy_c(p dt/dy)^2 HV_c$ 

### 2.3 Horizontal Momentum Diffusion

Assume that the equations of motion (1) and (2) contain a horizontal diffusion term on their right hand side as approximated by the classical Laplacian in Compass-Rose notation for (U,V) (assuming an equidistant grid with dx=dy=dl):

 $\begin{array}{ll} Ah \big( U_{xx} + U_{yy} \big) & \mbox{in (1);} & \mbox{approximation:} Ah \, (U_E + U_W + U_N + U_S - 4U_C)/dl^2 \\ Ah \big( V_{xx} + V_{yy} \big) & \mbox{in (2);} & \mbox{approximation:} \\ Ah \, (V_E + V_W + V_N + V_S - 4V_C)/dl^2 \end{array}$ 

We see that the difference stencil of the Laplacian 'grabs' at grid-points along main axes that are one increment apart from C, including the centre point C. What happens in an arbitrary topography if this Laplacian is in operation? It would eventually grab dry cells and draw in zero momentum...

### 2.4 Boundary Conditions for the Laplacian; Slip-conditions

The Laplacian simulates diffusion caused by lateral shear of the flow. It depends on lateral boundary conditions at coasts. We have to discern between 2 boundary conditions: a) the normal condition i.e. no flux across a closed boundary, and b) the 'noslip at a wall' condition, i.e. wall-parallel flow being zero at the wall (integral part of boundary layer theory).

Consider case a. (normal condition) in the C-grid:

$$wall$$

$$U_W \quad U_C \quad U_E = 0, (\text{no-flux})$$

$$\times \quad \times \quad \times$$

$$wet \quad wet \quad dry$$

In this example both Uw and Uc are wet, and Ue is dry i.e. =0 because it is situated at a closed boundary. These casesare consistent with the normal condition; they may enter the Laplacian without causing problems. The situation is different for coastal-normal derivatives of coastal parallel flow:

Consider case b. (no-slip condition) in the C-grid

Amongst other cells the Laplacian Operator  $(U_E + U_W + U_N + U_S - 4U_C)/dl^2$  for  $U_C$  grabs  $U_N$ , which is dry in this example. Between  $U_N$  and  $U_C$  is the wall at which the north-component V is zero, and at which U must be zero as well. To highlight that the Laplacian contains a differential of coastal parallel horizontal momentum shear we rewrite its meridional derivatives of shear as:  $(\tau_N - \tau_S)/dl$  in which, according to Newton's friction law  $\tau_N = Ah (U_N - U_C)/dl$  and  $\tau_S = Ah (U_S - U_C)/dl$ .

The example concerns the shear term  $\tau_N$  because it addresses a dry cell. Momentum component  $U_N$  in the above sketch must be zero for it lies on dry land, which implies  $\tau_N = -AhU_C/dl$ .

To fulfil the condition of a vanishing wall-parallel flow, i.e. 'no-slip' in the discrete grid  $U_N$  must be equal  $-U_C$ . Then their spatial average would exactly be zero at the wall. With components being equal yet having opposite sign  $\tau_N = -2AhU_C/dl$ , which complies with the 'no-slip' condition. Thus, vanishing wall-parallel flow implies maximal shear at the wall. A vanishing shear, i.e.  $\tau_N = 0$  at the wall requires that  $U_N$  is equal  $U_C$ . This would be a 'full-slip', elsewhere also called 'free-slip' condition.

Conservation of mass requires that all momentum cells on dry land are zero. It is not advisable to relax this condition. However, the control of lateral shear, i.e. slip in the Laplacian requires a modification of momentum-components. Thus, we have to devise an algorithm, which automatically implements a slip-condition whenever coastal parallel shear is present, and which still allows conserving mass. For this purpose we define wet/dry integer 'masks' for both momentum-components which are one if wet, otherwise zero. The masks allow discerning, i.e. switching between computations with the classical Laplacian in open water, i.e. away from a coast, and cases where coastal parallel shear occurs.

### 2.5 Coriolis Rotation; the Problem with spatial averaging in the C-grid

The inclusion of Coriolis rotation terms in the C-grid is a tedious task because momentum-components are not on the same location contrary to B- or E-grids. The approximation of rotation at a U-component for instance requires a spatial average of four surrounding V-components for the rotation matrix. This is the one disadvantage of the C-grid. That is, because in an arbitrary topography not all V-neighbours might be wet. In the worst case, i.e. when all four surrounding V-components are dry an application of the rotation matrix would induce unwanted damping.

An example for such a case is a topography that locally degenerates to a onedimensional channel; for instance between an island and the mainland:

Implementing rotation in open water, away from a coast implies that Un is replaced by the rotated U-component Urot in the approximation of the equation of motion:

 $\mathbf{U}^{n+1} = \mathbf{U}^n + \text{further terms} = \mathbf{U}^{n+1} = \mathbf{U}_{rot} + \text{further terms}$ 

Utilising spatial averages the rotated vector-components read:

### $\mathbf{U}_{rot} = \alpha \mathbf{U} + \beta \mathbf{V} \mathbf{a} t \mathbf{U}; \mathbf{V}_{rot} = \alpha \mathbf{V} + \beta \mathbf{U} \mathbf{a} t \mathbf{V}$

Now for the worst case with spatial average **VatU**being zero  $\mathbf{U}_{rot} = \boldsymbol{\alpha} \mathbf{U}$ , which will decrease U for  $\boldsymbol{\alpha}$  is less than one. Thus, rotation has become dissipation. In this event, the bilateral energy-transfer amongst components does not work because one is always zero. Only Conclusion: abandon rotation for this case to avoid damping.

The respective four neighbour-components for spatial averages (UatV, VatU) are: VatU: V(i, j) + V(i + 1, j) + V(i, j - 1) + V(i + 1, j - 1); UatV: U(i, j) + U(i, j + 1) + U(i - 1, j) + U(i - 1, j + 1);

Note inverse symmetry in the indexing. In an arbitrary topography, any one of the four cells might be dry and usage of averages irrespective of dry cells may underestimate averages. For instance if only two cells are wet and one divides by four. Thus, not only we have to decide whether rotation is possible but also to determine how many wet cells enter the average. We require that at least two wet cells be present in the average, otherwise rotation is abandoned.

Since the topography does not change in time, a counting of the number of wet cells for averages is done once, prior to the time-loop.

2D Tracer Advection in the C-grid

Once the model has produced new values of the velocity-vector (u,v) derived from momentum  $(\mathbf{U}, \mathbf{V})$  at time level n+1 a new distribution of tracers can be computed, here exemplified for a tracer S. Neither sources nor sinks are assumed.

$$dS/dt = \partial S/\partial t + u \,\partial S/\partial t + v \,\partial S/\partial y = 0. \tag{1}$$

Upstream advection-code (2) approximate (1):

 $S^{n+1}(i,j) =$ 

$$S^{n}(i,j) - \Delta t \, u_{W}^{n+1} / dx \big( S(i,j) - S(i-1,j) \big)^{n} - \Delta t \, u_{E}^{n+1} / dx \big( S(i+1,j) - S(i,j) \big)^{n} - \Delta t \, v_{S}^{n+1} / dx \big( S(i,j) - S(i,j-1) \big)^{n} - \Delta t \, v_{N}^{n+1} / dx \big( S(i,j+1) - S(i,j) \big)^{n}$$
(2)

In the advection scheme (2) we use upstream 'velocity-switches' as given below.

$$\begin{split} u_{W}^{n+1} &= \left(abs\big(u(i-1,j)\big) + u(i-1,j)\big)^{n+1}/2; u_{E}^{n+1} = \left(abs\big(u(i,j)\big) - u(i,j)\big)^{n+1}/2 \\ v_{S}^{n+1} &= \left(abs\big(v(i,j-1)\big) + v(i,j-1)\big)^{n+1}/2; v_{N}^{n+1} = \left(abs\big(v(i,j)\big) - v(i,j)\big)^{n+1}/2 \\ \end{array} \end{split}$$

Zonal arrangement of grid points in the staggered grid for tracer S:

$$S(i-1,j) \qquad S(i,j) \quad S(i+1,j)$$

$$+ \qquad \times \qquad + \qquad \times \qquad +$$

$$U_w \qquad U_E$$

note: uE has index (i,j) due to staggered grid

By defining non-dimensional coefficients:

$$\mathbf{C}_{\mathbf{E}} = \Delta \mathbf{t} \, \mathbf{u}_{\mathbf{E}} / \mathbf{d} \mathbf{x}; \mathbf{C}_{\mathbf{W}} = \Delta \mathbf{t} \, \mathbf{u}_{\mathbf{W}} / \mathbf{d} \mathbf{x}, \quad \text{and} \quad \mathbf{C}_{\mathbf{N}} = \Delta \mathbf{t} \, \mathbf{v}_{\mathbf{N}} / \mathbf{d} \mathbf{y}; \mathbf{C}_{\mathbf{S}} = \Delta \mathbf{t} \, \mathbf{v}_{\mathbf{S}} / \mathbf{d} \mathbf{y},$$

We can write the advection scheme (2) in the compact explicit form (3) where always two of the four coefficients are zero:

$$S_{C}^{n+1} = S_{C}^{n}(1 - C_{W} + C_{E} - C_{S} + C_{N}) + C_{W}S_{W}^{n} - C_{E}S_{E}^{n} + C_{S}S_{SW}^{n} - C_{N}S_{N}^{n}$$
(3)

Note: the compass rose indexing always assumes that C indicates the location at which a property is computed. The neighbourhood is indexed with reference to C.

Boundary conditions: at closed lateral boundaries, an advective flux of matter is prohibited. Thus, boundary conditions for advective horizontal fluxes are simply given by the fact that velocities are zero at closed boundaries. We can always check the correctness of the code in a closed domain: S must be conserved. That is, the sum over all S in wet cells must remain the same, i.e. dS/dt = 0.

Remark: We can interpret operator (3) as a weighted spatial average of the tracer property S. The operator only works along coordinate axes. Therefore, it is also called: 'Component Upstream'. Advection with a flow along grid diagonals or in curved flow is under-represented by the simple Component Upstream scheme, and induces strong lateral diffusion. To overcome this disadvantage we introduce an additional cell at the grid diagonal to improve upstream interpolation. Then it would only utilise three cells in a triangle.

Modifying component upstream to triangular upstream with the intention to obtain a better estimate of the advected property causes a numerical approximation that is non-consistent. With spatial and time-increments approaching zero the scheme would not converge to the original partial differential equation. Thus, the below example for an improved advection scheme suffers from non-consistency. We call it 'Lagrangian Advection Scheme' (LAS). However, even though LAS is non-consistent it produces much better results and is as conservative as component upstream. The same finding applies for the rotation matrix, which again, is non-consistent.

### 2.6 The Lagrangian upstream Advection Scheme, LAS:

The idea of LAS is to interpolate a property that lies upstream which, when advected with the flow during one time-step will end up at (i,j) where its value replaces tracer S(i,j). Below is an example of a routine that computes weights for interpolation in an upstream triangle. It uses non-dimensional excursions (cx,cy), i.e. the upstream location of the tracer:

$\mathbf{c}\mathbf{x} =  \overline{\mathbf{u}}   \mathbf{d}\mathbf{t}/\mathbf{d}\mathbf{x}$	with	$\overline{\mathbf{u}} = (\mathbf{u}_{\mathrm{E}} + \mathbf{u}_{\mathrm{W}})/2$
$\mathbf{c}\mathbf{y} =  \overline{\mathbf{v}}   \mathbf{d}\mathbf{t}/\mathbf{d}\mathbf{y}$	with	$\bar{v}=(v_N+v_S)/2$

 $(\bar{\mathbf{u}}, \bar{\mathbf{v}})$  are velocities centred on the tracer grid point at (i,j). Increments (idel, jdel), with deviations +/-1 define the respective quadrant out of four around (i,j) = LOCL in which interpolation will take place. Thus, with (idel, jdel) = (-1,-1) it would be the southwest quadrant. The minus signs in formulae for (idel, jdel) address the upstream quadrant:

 $idel = -sign(1, \overline{u}); \quad jdel = -sign(1, \overline{v})$ 

The four quadrants around LOCL:

+ DGNL + JDEL + DGNL

+ IDEL + LOCL + IDEL

+ DGNL + JDEL + DGNL

Routine 'trint' decides about the sub-triangle within a chosen quadrant. It produces four weights for triangular interpolation, where one of which will be zero, either  $w_{IDEL}$ or  $w_{JDEL}$ , depending on the ratio cx versus cy. With the four weights  $w_{LOCL}$ ,  $w_{IDEL}$ ,  $w_{JDEL}$ ,  $w_{DGNL}$  produced by trint we can write our advection problem as a weighted spatial interpolation in which the sum of all weights is one:

 $S(i, j)^{n+1} = w_{LOCL}S(i, j)^n + w_{IDEL}S(i + IDEL, j)^n + w_{JDEL}S(i, j + JDEL)^n + w_{DGNL}S(i + IDEL, j + JDEL)^n$ 

(4)

The interpolated upstream property  $S(i, j)^{n+1}$  obtained from (4) replaces the tracer S at location (i,j). This simulates Lagrangian advection. Note the result of this advectionalgorithm directly delivers the desired new tracer value. That is because only one process, i.e. advection governs the prognostic equation. In the equations of motion however, there is generally more than just one term contributing to a solution at time-level n+1. Thus, as we will see below for momentum advection, the result of LAS is then converted to a temporal change  $\Delta$ S:

 $\Delta \mathbf{S}(\mathbf{i},\mathbf{j})^{n+1} = \mathbf{S}(\mathbf{i},\mathbf{j})^{n+1} - \mathbf{S}(\mathbf{i},\mathbf{j})^n$ 

### 2.7 Non-linear advective Terms in the Equations of motion

Above we have seen the straightforward implementation of the triangular Lagrangian Advection scheme (LAS) for a scalar tracer. Including non-linear (advective) terms for momentum advection  $\mathbf{U}_t = \mathbf{u}\mathbf{U}_x + \mathbf{v}\mathbf{U}_y$ ;  $\mathbf{V}_t = \mathbf{u}\mathbf{V}_x + \mathbf{v}\mathbf{V}_y$  in the equations of motion implies applying LAS to both momentum-components. We need estimates of spatially averaged advection velocities ( $\mathbf{\bar{u}}, \mathbf{\bar{v}}$ ) similar as for the tracer. As seen for the scalar tracer LAS delivers the new tracer value at location (i,j) caused by advection. However, in our equations of motion there are a number of terms not just one. Their addition to  $\mathbf{U}^n$  or  $\mathbf{U}_{rot}$ , respectively yields the final result at time-level n+1. All of these terms deliver temporal changes, which we add to a component at time-level n to yield the result at n+1. We obtain a temporal advective change  $\Delta \mathbf{U}_{adv}$  by subtracting  $\mathbf{U}^n$  from

 $\mathbf{U}_{adv}$  delivered by LAS:  $\Delta \mathbf{U}_{adv} = \mathbf{U}_{adv} - \mathbf{U}^{n}$ . In the below coding we, therefore subtract unity from the center-coefficient  $\mathbf{w}_{LOCL}$  for  $\mathbf{U}^{n}$  which delivers  $\Delta \mathbf{U}_{adv}$ , i.e. 'momadv\_u'.

### 2.8 Stability of the rotational nonlinear 2D C-grid model

Three stability criteria apply to the numerical scheme of our explicit model, and all three my not be violated to obtain a stable simulation. Re-iterating stability criteria:

- The CFL-criterion for the free surface:  $\Delta t \leq \Delta L / \sqrt{2^{n-1}gH}$
- The criterion for the heat conduction (diffusion) equation:  $\Delta L^2 > 2^n A h \Delta t$
- The Courant-Number for tracer/momentum advection:  $c\Delta t/\Delta L \leq 1$

Advection velocity  $\mathbf{c} = \mathbf{max}(|\mathbf{u}|, |\mathbf{v}|)$ , n=2 (for 2D model),  $\mathbf{H} = \mathbf{max}(\mathbf{D} + \boldsymbol{\zeta})$  in domain, and  $\Delta \mathbf{L} = \min(d\mathbf{x}, d\mathbf{y})$ , Ah turbulent horizontal exchange coefficient (m<sup>2</sup>/s).

### 3 Implicit Channel Model with 'Movable' Boundary

The technique to simulate a 'movable boundary' was originally developed for simulations of tidal dynamics in the Wadden Sea where large areas of the sea floor are exposed during ebb tide. With the incoming flood, banks and mud flats are inundated due to flooding i.e. the land/water interface moves with time and space. In a numerical model, this can only be achieved by introducing a 'movable boundary'. For twodimensional cases, models with a movable boundary may simulate inundation that is caused by a tsunami wave. They have also successfully been used to simulate bottom arrested gravity plumes i.e. subsea avalanches of dense seawater or sediment-enriched water in a rotational framework. Here we demonstrate and explain the technique of the 'movable boundary' in a one-dimensional problem. It allows extending the model to a two-dimensional one.



Figure 2: flooding and drying in a 1D implicit channel model; hourly sequence of tidal surface elevations

Generally in ocean models lateral boundaries i.e. coasts are fixed and do not change location with time. However, all over the world, in the rhythm of tides, a flooding and drying of shallow coastal regions occurs. In Europe, this happens in the English Channel, the Bay of Biscay, and in the German Bight of the North Sea, i.e. in the 'Wadden Sea'. In these regions, the land/water interface moves laterally with flood and ebb tide thereby exposing vast areas of the seabed to the atmosphere twice a day. A closed boundary implies application of the 'normal condition', i.e. no flux through a wall. To simulate flooding and drying of coastal wetlands the 'rigid', or stringent application of the 'normal condition' has to be relaxed in order to arrive at a 'movable' closed boundary whereby the latter may move only one spatial increment per time step.

To achieve this we define logical criteria for flooding conditions. In dry points of our channel, the surface elevation  $\zeta$  aligns with the seabed like a membrane that sticks to it. The distance between membrane and seabed is defined by a 'critical depth' Hcrit, normally a few centimeters. In case of flooding water lifts the membrane off the seabed. The drying of a cell occurs whenever the actual water depth  $\mathbf{H} = \mathbf{D} + \zeta$  becomes equal or smaller than the critical depth  $\mathbf{H}_{crit}$ . That is, in dry cells  $\mathbf{H} \leq \mathbf{H}_{crit}$  whereas in wet cells  $\mathbf{H} > \mathbf{H}_{crit}$ . At any time (step) the wet/dry pattern of the model domain must be determined anew. To simulate the 'movable' lateral boundary only the flooding needs special treatment because the drying is given by a falling surface elevation approaching the seabed until  $\mathbf{H} < \mathbf{H}_{crit}$ . With too large a time step, H might become smaller than

zero, which implies 'virtual water'. We simulate the movable boundary by a simple intuitive, yet remarkably efficient algorithm based on Boolean Logics.

### **3.1** Flooding towards the west

Normally i.e. without a movable boundary a U-component surrounded by two dry pressure cells must be considered as being 'dry' (U=0). At pressure cells the actual water depth H is defined. In allowing for a movable boundary, this condition is relaxed under certain circumstances. Consider the case where all cells to the west of the arrow are dry. There the membrane i.e. surface elevation  $\boldsymbol{\zeta}$  hugs the seabed.



Figure 3: flooding towards the west

To the right of the arrow water moves westward and lifts the membrane off the sea floor. At the dry U-component (arrow) a decision has to be made to allow water to flood cell 'w'. This can only occur if the dry U-component is 'wetted'. That is, Criterion 'Flood to West' expressed in Boolean Logics must apply:

 $H_w < H_{crit}$  and  $H_e > H_{crit}$  and  $(\zeta_e - \zeta_w)/\Delta x > \Delta \zeta_{crit}$  with  $\Delta \zeta_{crit} = H_{crit}/\Delta x$ 

In the above graph, the western cell is dry, and the eastern is wet. Normally both cells need be wet to allow computing the U-component (arrow). Here, in order to enable a flooding we check whether there is a flow in the eastern cell directed into the dry cell. Thus, with the eastern cell being wet we need a surface elevation that causes a pressure gradient that forces a flow into the dry cell as expressed by the 'Flood to West' Criterion. Should the criterion not apply the U-component (arrow) would remain dry, i.e. no flow through a closed boundary. In case flooding was diagnosed the equation of motion would be solved with  $U^n = 0$ , i.e. no friction, and with the only forcing arising from the sea level gradient between cells w and e.
## 3.2 Flooding towards the east

To allow for a flooding towards the east the following situation must apply: eastern cell is dry, western is wet and the slope of the surface elevation must be negative for forcing a flow into the eastern cell. Thus, the 'Flood to East' Criterion reads:

 $H_e < H_{crit} ~\text{and}~ H_w > H_{crit}~\text{and}~ (\zeta_e - \zeta_w)/\Delta x < -\Delta \zeta_{crit}$ 

## List of Figures

Figure 1: Bathymetry of the PG region (numerical model domain). The present model forced at the southern open boundary. 10

Figure 2: Schematic of the surface circulation in the PG expounded in Reynolds (1993). The dashed lines in the central part of the PG indicate the approximate seasonal location of the water mass front between fresh water of the Gulf of Oman and the more saline water of the PG. 14

Figure 3: The topography of the PG (colorbar in meter), provided from data source GEBCO\_08 Grid version 20100927, by the General Bathymetric Chart of the oceans from the British Oceanographic Data Centre. 19

Figure 4: Bathymetry of the region of PG. The numbers with white background indicate the location of tidal gauges listed in table 1. Data of red bullet locations is provided by Iranian National Cartographic Center and blue is provided by International Hydrographic Office. The numbers with yellow background indicate the depth of contours in meters. 21

Figure 5: Comparison of Model and Observation for harmonics constants for M2, K1, and S2 in the PG. 23

Figure 6: Comparison of Model and Observation for tidal constituents of O1, N2, and P1 in the PG. 24 Figure 7: Comparison between, the OTIS regional tidal solution and Observation for 8 harmonic constants in the PG, obtained by harmonic analysis of the data provided by Iranian National Cartographic Center. 24

25

30

Figure 8: Model Result for factor F over the PG.

Figure 9: Model Result for M2 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers 26 Figure 10: Model Result for K1 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers 26 Figure 11: Model Result for S2 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers. 27 Figure 12: Model Result for O1 Co-Tidal lines over the PG. Co- Amplitude lines are dash lines with framed numbers and Co- Phase lines are normal lines with no frame numbers. 27 Figure 13: Model Result for M2 maximum velocities over the PG in m/s. 28 Figure 14: Model Result for K1 maximum velocities over the PG in m/s. 28 Figure 15: Model result for M2 tidal ellipses in the PG. Blue ellipses rotate clockwise and red ellipses

Figure 16: Model result for K1 tidal ellipses in the PG. Blue ellipses rotate clockwise and red ellipses rotate anticlockwise.

rotate anticlockwise.

Figure 17: Maximum tidal currents velocity (colorbar in m/s) in the PG using 13 tidal constituents at the open boundary. 32

Figure 18: Kinetic power density (colorbar in  $kW/m^2$ ) from the tidal current. 33

Figure 19: Effect of Qeshm canal on the tidal solution with single harmonic forcing (M2) at the open Boundary, Model Result for tidal range difference of M2 amplitude in two conditions; closed canal and real topography in cm (real-closed).

Figure 20: High-pass filtered topography of the PG in meters (colorbar). Box 1 indicates the area zoomed in Figure 28.

Figure 21: Residual current ( $\times 10^{-3}$  m/s) pattern around a symmetric hill. The current direction of approach flow is northward. The background and vectors display the Residual currents. White contours are the topography contours. 40

Figure 22: Residual vorticity ( $\times 10^{-6}$  s<sup>-1</sup>) pattern around a symmetric hill (left) and a valley (right). The current direction of approach flow is northward. 41

Figure 23: Residual current ( $\times 10^{-3}$ m/s) pattern around an elongated hill (left). The background and vectors display the Residual currents. White contours are the topography contours. Residual vorticity ( $\times 10^{-5}$  s<sup>-1</sup>) pattern around a symmetric hill (right). The current direction of approach flow is northward.

Figure 24: Residual current ( $\times 10^{-3}$ m/s) pattern around an elongated and tilted hill (left). The background and vectors display the Residual currents. White contours are the topography contours. The residual vorticity ( $\times 10^{-5}$  s<sup>-1</sup>) pattern around an elongated and tilted hill (right). The current direction of approach flow is northward. 41

Figure 25: The residual current around a hill and a valley. Wide arrows are the current direction of approach flow. The background contours display the topography. For a hill, water depth decreases to the center and for a valley, it increases. Gyres illustrate the direction of residual current around the topography contours. Looking in the direction of the flow cyclonic and anticyclonic gyres are on different sides in the case of a hill and a valley. 42

Figure 26: Model Result for K1 residual velocity (m/s) in the PG. 43

Figure 27: Model Result for M2 residual velocity (m/s) in the PG.

Figure 28: M2 Residual current vectors around a hill in high-pass filtered topography (colorbar in meters) of the PG. vectors show the M2 residual currents. CD is the Current Direction. This area is shown in Figure 1 with Box 1. 45

Figure 29: Lagrangian trajectories (black lines) in residual vorticity (colorbar  $\times 10^{-5}$  s<sup>-1</sup>), running with residual velocities of M2+S2+K1+O1 for 120 days. 46

Figure 30: Lagrangian trajectories (black lines) in residual vorticity (colorbar  $\times 10^{-5}$  s<sup>-1</sup>), running with residual velocities of M2+S2+K1+O1 for 120 days. Green lines show 2 main gyres in the PG. The red box in guide map shows the position of zoomed figure in the PG. 46

43

Figure 31: Box 1 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points. 47

Figure 32: Box 2 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points. 48

Figure 33: Box 3 of trajectories running with residual velocities of M2+S2+K1+O1 for 120 days. Gray marks are the start points.

Figure 34: a) The topography of the PG, contour lines with an increment of 20 m. Y-axis: latitude; X-axis: longitude. b) Displacement of amphidromic points with different periods of forcing (10 h to 35 h), Blue circles: periods with 2 amphidromic points, Red circles: periods with a single amphidromic point. c) The position of monitoring stations; N1-N4 stations in the northern PG, S1-S4 stations in southern PG, H1-H4 stations in Strait of Hormuz. Data at monitoring stations are shown in Figures 39, 40 and 41.

Figure 35: Tidal amplification factor (colorbar) for the period of 12.5 h in the PG. Y-axis: latitude; X-axis: longitude.

Figure 36: Tidal amplification factor (colorbar) for the period of 24 h in the PG. Y-axis: latitude; Xaxis: longitude. 55

Figure 37: Periods (from 3.5 h to 35.5 h) of maximum tidal ranges in the PG. Y-axis: latitude; X-axis: longitude; Colorbar: Period in hours. 55

Figure 38: Maximum tidal amplification factor (colorbar) from period 3.5 h to 35.5 h in the PG. The neutral tidal amplification factor is shown by the contour. Y-axis: latitude; X-axis: longitude. 56 Figure 39: Tidal amplification factor for the monitoring points, N1-N4, in the northern PG (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines. 57

Figure 40: Tidal amplification factor for the monitoring points, H1-H4, in the Strait of Hormuz (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines. 58 Figure 41: Tidal amplification factor for the monitoring points, S1-S4, in the region off the Arabian coast (See figure 3 for positions). Periods of the main tides (M2, S2, O1, and K1) are marked as dash lines. 58

Figure 42: Increase of tidal amplification factor (colorbar) for the period of 12.5 h due to sea level rise of 1 m in the PG. Y-axis: latitude; X-axis: longitude.

Figure 43: Increase of tidal amplification factor (colorbar) for the period of 24 h due to sea level riseof 1 m in the PG. Y-axis: latitude; X-axis: longitude.60

Figure 44: The annual potential power density (colorbar in MW/cell) of the semidiurnal tide. 61

Figure 45: The annual potential power density (colorbar in MW/cell) of the diurnal tide.61Figure 46: satellite picture of the Musa estuary.63

Figure 47: The topography of the Musa estuary (colorbar in meter). Redline shows the track line along the main channel.

Figure 48: Different layers from satellite picture and measurement data, used for creating the
topography of the Musa estuary. 65
Figure 49: Schematic diagram of heat fluxes on tidal flats. Arrows indicate the direction of heat flux.
65
Figure 50: total salt in the domain, the output of salt from the open boundary and tidal elevation of the
open boundary for 140 simulation days. 66
Figure 51: Total salt in the domain, the output of salt from the open boundary and tidal elevation of
the open boundary for the last 20 days of 140 days. 67
Figure 52: Tidally-averaged current velocity (colorbar in m/s) on the slope without the effect of
thermodynamics. Vectors show the direction of the currents. 68
Figure 53: Tidally-averaged current velocity (colorbar in m/s) on the slope with the effect of
thermodynamics. Vectors show the direction of the currents. 69
Figure 54: Density-driven currents (colorbar in m/s) on the slop, the difference between Figure 52 and
Figure 53. Vectors show the direction of the currents.69
Figure 55: Model results for salinity (colorbar) after 120 days and 1 hour, UL: Surface layer. UR:
Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL. 70
Figure 56: Model results for salinity (colorbar) after 120 days and 5 hours, UL: Surface layer. UR:
Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL. 71
Figure 57: Model results for salinity (colorbar) after 120 days and 9 hours, UL: Surface layer. UR:
Section M163. LL: Section Z093. LR: Section M316. Sections are marked with three lines in UL. 71
Figure 58: Model results after 120 days and 12 hours for section Z093 in Musa estuary. Left: salinity
(colorbar). Right: V-component of current velocity (colorbar in m/s). The section is marked in Figure
55. 72
Figure 59: Model results after 120 days and 18 hours for section Z093 in Musa estuary. Left: salinity
(colorbar). Right: V-component of current velocity (colorbar in m/s). The section is marked in Figure
55. 72
Figure 60: Model results after 120 days and 12 hours for section M163 in Musa estuary. Left: salinity
(colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure
55. 73
Figure 61: Model results after 120 days and 12 hours for section M163 in Musa estuary. Left: salinity
(colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure
55. 73
Figure 62: Model results after 120 days and 12 hours for section M316 in Musa estuary. Left: salinity
(colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure

55.

74

Figure 63: Model results after 120 days and 12 hours for section M316 in Musa estuary. Left: salinity (colorbar). Right: U-component of current velocity (colorbar in m/s). The section is marked in Figure 55. 74

Figure 64: Tidally-averaged salinity, (colorbar) along the track in the Musa estuary.75Figure 65: Tidally-averaged current velocity (colorbar in m/s), in the direction of the track in the<br/>Musa estuary.75

Figure 66: Tidally-averaged current velocity (colorbar in m/s), normal to the direction of the track in the Musa estuary. 76

Figure 67: The model results in the meridional (M324) section in the Musa estuary for, Left: Tidallyaveraged current velocity (colorbar in m/s), normal to the section, positive means inflow. Right: Tidally-averaged salinity (colorbar). 76

Figure 68: The model results in the zonal (Z036) section in the Musa estuary for, Left: Tidallyaveraged current velocity (colorbar in m/s), normal to the section, positive means inflow. Right: Tidally-averaged salinity (colorbar). 77

## List of Tables

Table 1: List of tide gauges used if Figures 5. First 4 stations are provided by Iranian NationalCartographic Center and others are provided by International Hydrographic Office.21Table 2: Comparison between Model and Observation for tidal constituents of M2, K1, S2, O1, N221and P1 in the PG. Phases are in degrees from Greenwich.22

## List of publications

- Mashayekh Poul, H., Backhaus, J.O., Huebner, U., 2014. Estimate the area with most efficiency for producing energy from tide in the Persian Gulf, in: The 11th International Conference on Coasts, Ports and Marine Structures.
- Mashayekh Poul, H., Backhaus, J., Huebner, U., 2016. A description of the tides and effect of Qeshm canal on that in the Persian Gulf using two-dimensional numerical model. Arabian Journal of Geoscience, 9, 148. doi:10.1007/s12517-015-2259-8
- Mashayekh Poul H., Backhaus J., Dehghani, A., Huebner, U., 2016. Effect of subseabed salt domes on Tidal Residual currents in the Persian Gulf. Journal of Geophysical Research Ocean 121:3372–3380. doi: 10.1002/2015JC011421